



Please write clearly in block capitals.

Centre number

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Candidate number

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Surname

Forename(s)

Candidate signature

I declare this is my own work.

AS FURTHER MATHEMATICS

Paper 2 Discrete

Friday 17 May 2024

Afternoon

Time allowed: 1 hour 30 minutes

Materials

- You must have the AQA Formulae and statistical tables booklet for A-level Mathematics and A-level Further Mathematics.
- You should have a graphical or scientific calculator that meets the requirements of the specification.
- You must ensure you have the other optional Question Paper/Answer Book for which you are entered (**either** Mechanics **or** Statistics). You will have 1 hour 30 minutes to complete **both** papers.

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer each question in the space provided for that question. If you require extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do **not** write outside the box around each page or on blank pages.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 40.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.

For Examiner's Use	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
8	
9	
10	
TOTAL	



J U N 2 4 7 3 6 6 2 D 0 1

G/LM/Jun24/G4001/V4

7366/2D

Answer **all** questions in the spaces provided.

1 A connected planar graph has v vertices, e edges and f faces.

Which one of the formulae below is correct?

Circle your answer.

[1 mark]

$$v + e + f = 2$$

$$v - e + f = 2$$

$$v - e - f = 2$$

$$v + e - f = 2$$

2 Find an expression for the number of edges in the complete bipartite graph, $K_{m,n}$

Circle your answer.

[1 mark]

$$\frac{m}{n}$$

$$m - n$$

$$m + n$$

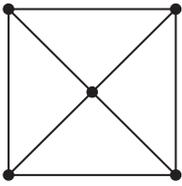
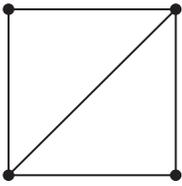
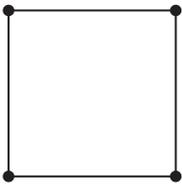
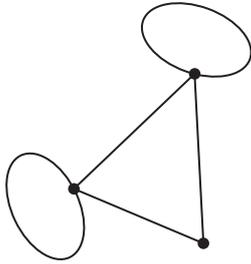
$$mn$$



3 Which one of the graphs shown below is semi-Eulerian?

Tick (✓) **one** box.

[1 mark]



Turn over ►



4 The set S is defined as $S = \{1, 2, 3, 4\}$

4 (a) Complete the Cayley Table shown below for S under the binary operation multiplication modulo 5

[2 marks]

\times_5	1	2	3	4
1				
2				
3				
4				

4 (b) State the identity element for S under multiplication modulo 5

[1 mark]

4 (c) State the self-inverse elements of S under multiplication modulo 5

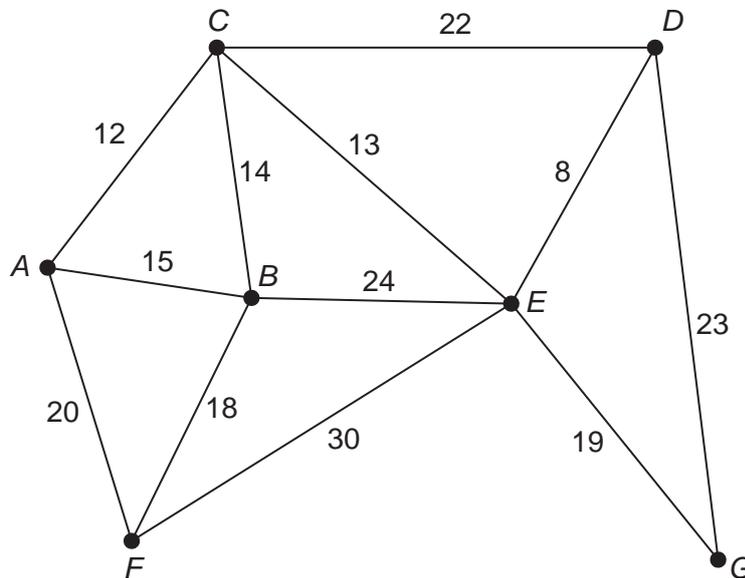
[1 mark]



5 A network of roads connects the villages A , B , C , D , E , F and G

The weight on each arc in the network represents the distance, in miles, between adjacent villages.

The network is shown in the diagram below.



5 (a) Draw, in the space below, the spanning tree of minimum total length for this road network.

[3 marks]

5 (b) Find the total length of the spanning tree drawn in part (a).

[1 mark]

Turn over ►



7 The binary operation ∇ is defined as

$$a \nabla b = a + b + ab \text{ where } a, b \in \mathbb{R}$$

7 (a) Determine if ∇ is commutative on \mathbb{R}

Fully justify your answer.

[2 marks]

7 (b) Prove that ∇ is associative on \mathbb{R}

[3 marks]

Turn over ►



8 (b) (i) State the value of y

[1 mark]

8 (b) (ii) State the value of z

[1 mark]

8 (c) Prove that the maximum flow through the network is at most $27 \text{ m}^3 \text{ s}^{-1}$

[2 marks]

Turn over ►



- 9** Robert, a project manager, and his team of builders are working on a small building project.

Robert has divided the project into ten activities labelled *A, B, C, D, E, F, G, H, I* and *J* as shown in the precedence table below:

Activity	Immediate Predecessor(s)	Duration (Days)
<i>A</i>	None	1
<i>B</i>	None	1
<i>C</i>	<i>A</i>	10
<i>D</i>	<i>A</i>	2
<i>E</i>	<i>B, D</i>	5
<i>F</i>	<i>E</i>	6
<i>G</i>	<i>E</i>	1
<i>H</i>	<i>F</i>	1
<i>I</i>	<i>F</i>	2
<i>J</i>	<i>C, G, H, I</i>	4

- 9 (a)** On the opposite page, construct an activity network for the project and fill in the earliest start time and latest finish time for each activity.

[4 marks]

- 9 (b)** Robert claims that the project can be completed in 20 days.

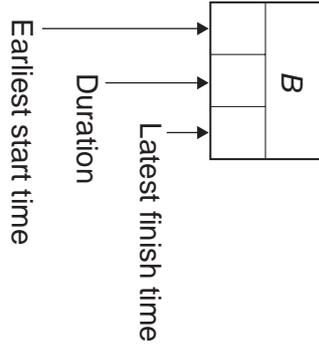
Comment on the validity of Robert's claim.

[2 marks]



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box

A	



Turn over for the next question

Turn over ►



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outside the
box*

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ANSWER IN THE SPACES PROVIDED**



