



Please write clearly in block capitals.

Centre number

Candidate number

Surname

Forename(s)

Candidate signature

I declare this is my own work.

A-level MATHEMATICS

Paper 3

Tuesday 20 June 2023

Afternoon

Time allowed: 2 hours

Materials

- You must have the AQA Formulae for A-level Mathematics booklet.
- You should have a graphical or scientific calculator that meets the requirements of the specification.

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer each question in the space provided for that question.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do **not** write outside the box around each page or on blank pages.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 100.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.

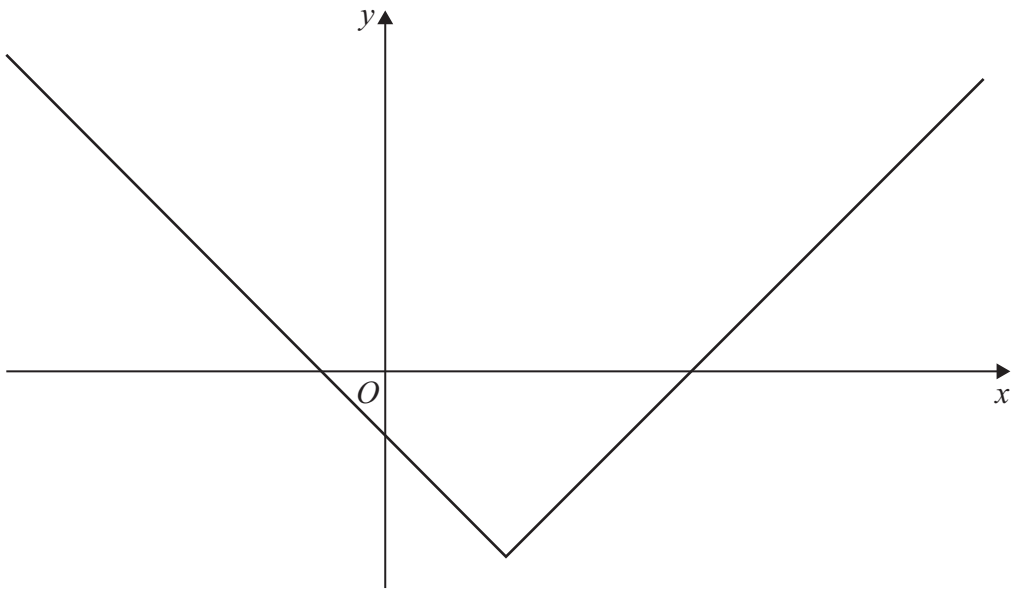
For Examiner's Use	
Question	Mark
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Section A

Answer **all** questions in the spaces provided.

1 The graph of $y = f(x)$ is shown below.



One of the four equations listed below is the equation of the graph $y = f(x)$

Identify which one is the correct equation of the graph.

Tick (✓) **one** box.

[1 mark]

$y = |x + 2| + 3$

☐

$y = |x + 2| - 3$

☐

$y = |x - 2| + 3$

☐

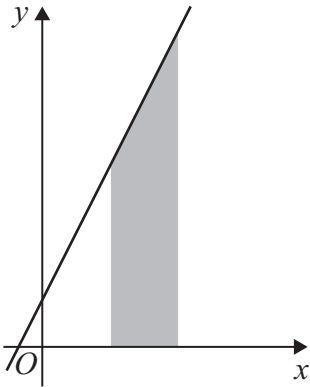
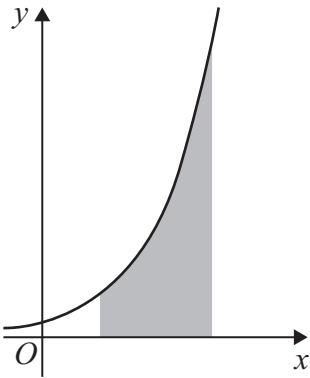
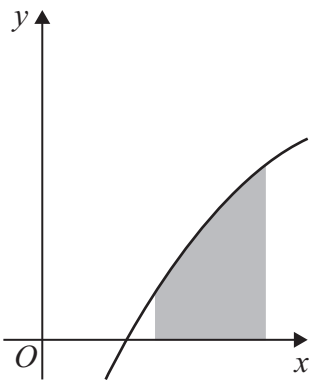
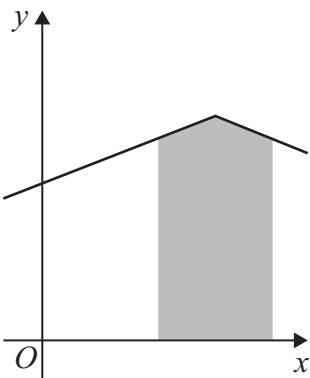
$y = |x - 2| - 3$

☐

2 The trapezium rule is used to estimate the area of the shaded region in each of the graphs below.
Identify the graph for which the trapezium rule produces an overestimate.

Tick (✓) **one** box.

[1 mark]

☐☐☐☐

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3 A curve with equation $y = f(x)$ passes through the point (3, 7)
Given that $f'(3) = 0$ find the equation of the normal to the curve at (3, 7)
Circle your answer.

[1 mark]

$y = \frac{7}{3}x$

$y = 0$

$x = 3$

$x = 7$

4 Express

$$\frac{5 - \sqrt[3]{x}}{x^2}$$

in the form

$$5x^p - x^q$$

where p and q are constants.

[2 marks]



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5 A curve has equation $y = 3e^{2x}$

Find the gradient of the curve at the point where $y = 10$

[3 marks]

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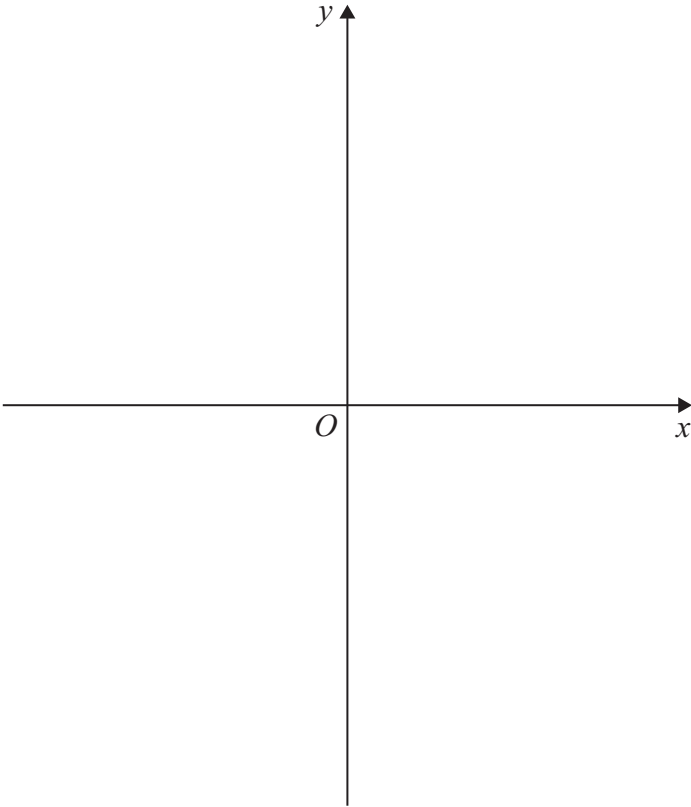
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6 (a) Sketch the curve with equation

$$y = x^2(2x + a)$$

where $a > 0$

[3 marks]



6 (b) The polynomial $p(x)$ is given by

$$p(x) = x^2(2x + a) + 36$$

6 (b) (i) It is given that $x + 3$ is a factor of $p(x)$

Use the factor theorem to show $a = 2$

[2 marks]



6 (b) (ii) State the transformation which maps the curve with equation

$$y = x^2(2x + 2)$$

onto the curve with equation

$$y = x^2(2x + 2) + 36$$

[2 marks]

6 (b) (iii) The polynomial $x^2(2x + 2) + 36$ can be written as $(x + 3)(2x^2 + bx + c)$

Without finding the values of b and c , use your answers to parts **(a)** and **(b)(ii)** to explain why

$$b^2 < 8c$$

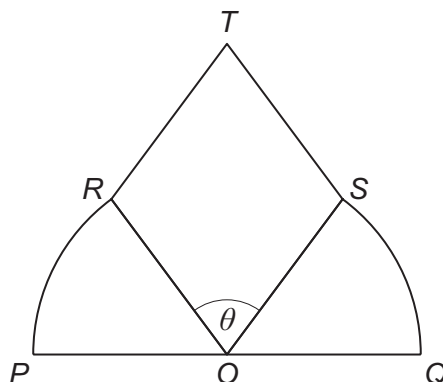
[2 marks]

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7 A new design for a company logo is to be made from two sectors of a circle, ORP and OQS , and a rhombus $OSTR$, as shown in the diagram below.



The points P , O and Q lie on a straight line and the angle ROS is θ radians.

A large copy of the logo, with $PQ = 5$ metres, is to be put on a wall.

7 (a) Show that the area of the logo, A square metres, is given by

$$A = \frac{25}{8}(\pi - \theta + 2 \sin \theta)$$

[4 marks]

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7 (b) (ii) Find the exact maximum value of A

[2 marks]

7 (c) Without further calculation, state how your answers to parts (b)(i) and (b)(ii) would change if PQ were increased to 10 metres.

[2 marks]



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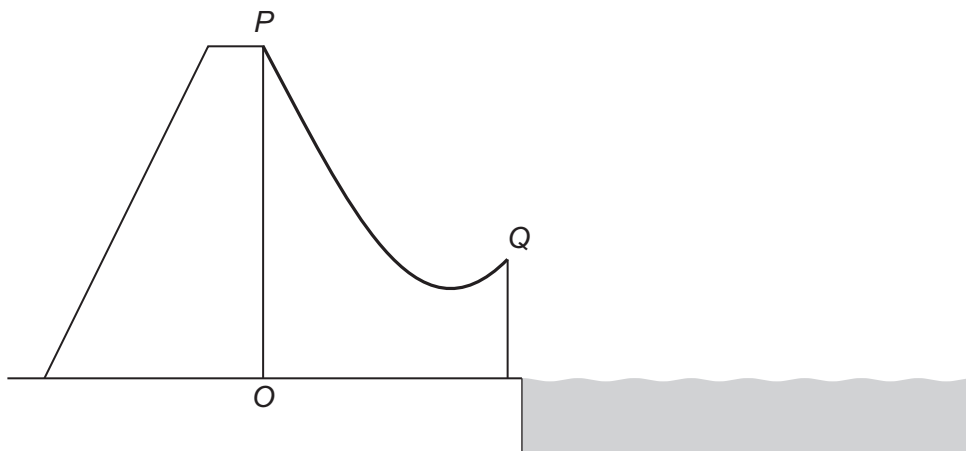
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- 9 A water slide is the shape of a curve PQ as shown in **Figure 1** below.

Figure 1



The curve can be modelled by the parametric equations

$$x = t - \frac{1}{t} + 4.8$$

$$y = t + \frac{2}{t}$$

where $0.2 \leq t \leq 3$

The horizontal distance from O is x metres.

The vertical distance above the point O at ground level is y metres.

P is the point where $t = 0.2$ and Q is the point where $t = 3$



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9 (b) (iii) Find the acute angle the slide makes with the horizontal at Q

Give your answer to the nearest degree.

[2 marks]

END OF SECTION A
TURN OVER FOR SECTION B

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Section B

Answer **all** questions in the spaces provided.

10 Which of the following is **not** a possible value for a product moment correlation coefficient?

Circle your answer.

[1 mark]

$$-\frac{6}{5}$$

$$-\frac{3}{5}$$

$$0$$

$$1$$

11 A and B are mutually exclusive events.

Which one of the following statements must be correct?

Tick (✓) **one** box.

[1 mark]

$$P(A \cup B) = P(A) \times P(B)$$

☐

$$P(A \cup B) = P(A) - P(B)$$

☐

$$P(A \cap B) = 0$$

☐

$$P(A \cap B) = 1$$

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12 It is known that, on average, 40% of the drivers who take their driving test at a local test centre pass their driving test.

Each day 32 drivers take their driving test at this centre.

The number of drivers who pass their test on a particular day can be modelled by the distribution B (32, 0.4)

12 (a) State one assumption, in context, required for this distribution to be used. **[1 mark]**

12 (b) Find the probability that exactly 7 of the drivers on a particular day pass their test. **[1 mark]**

12 (c) Find the probability that, at most, 16 of the drivers on a particular day pass their test. **[1 mark]**

12 (d) Find the probability that more than 12 of the drivers on a particular day pass their test. **[2 marks]**



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12 (e)

Find the mean number of drivers per day who pass their test.

[1 mark]

12 (f)

Find the standard deviation of the number of drivers per day who pass their test.

[2 marks]

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13 There are two types of coins in a money box:

- 20% are bronze coins
- 80% are silver coins

Craig takes out a coin at random and places it back in the money box.

Craig then takes out a second coin at random.

13 (a) Find the probability that both coins were of the same type.

[2 marks]

13 (b) Find the probability that both coins are bronze, given that at least one of the coins is bronze.

[2 marks]



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14 (c) A member of the council claims that if a different sample of 24 days had been used the hypothesis test in part **(b)** would have given the same result.

Comment on the validity of this claim.

[2 marks]

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15 (a) A random sample of eight cars was selected from the Large Data Set.

The masses of these cars, in kilograms, were as follows.

950 989 1247 1415 1506 1680 1833 2040

It is given that, for the population of cars in the Large Data Set:

lower quartile = 1167

median = 1393

upper quartile = 1570

15 (a) (i) It was decided to remove any of the masses which fall outside the following interval.

$$\text{median} - 1.5 \times \text{interquartile range} \leq \text{mass} \leq \text{median} + 1.5 \times \text{interquartile range}$$

Show that only one of the eight masses in the sample should be removed.

[3 marks]

15 (a) (ii) Write down the statistical name for the mass that should be removed in part **(a)(i)**.

[1 mark]



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15 (c) An expert team is investigating whether there have been any changes in CO₂ emissions from all cars taken from the Large Data Set.

The team decided to collect a quota sample of 200 cars to reflect the different years and the different makes of cars in the Large Data Set.

15 (c) (i) Using your knowledge of the Large Data Set, explain how the team can collect this sample. **[2 marks]**

15 (c) (ii) Describe **one disadvantage** of quota sampling. **[1 mark]**



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16 A farm supplies apples to a supermarket.

The diameters of the apples, D centimetres, are normally distributed with mean 6.5 and standard deviation 0.73

16 (a) (i) Find $P(D < 5.2)$ **[1 mark]**

16 (a) (ii) Find $P(D > 7)$ **[1 mark]**

16 (a) (iii) The supermarket only accepts apples with diameters between 5 cm and 8 cm.
Find the proportion of apples that the supermarket accepts. **[1 mark]**



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