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Centre number

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Candidate number

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Surname

Forename(s)

Candidate signature

I declare this is my own work.

A-level MATHEMATICS

Paper 1

Tuesday 6 June 2023

Afternoon

Time allowed: 2 hours

Materials

- You must have the AQA Formulae for A-level Mathematics booklet.
- You should have a graphical or scientific calculator that meets the requirements of the specification.

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer each question in the space provided for that question.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do **not** write outside the box around each page or on blank pages.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 100.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.

For Examiner's Use	
Question	Mark
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Answer **all** questions in the spaces provided.

1 Find the coefficient of x^7 in the expansion of $(2x - 3)^7$

Circle your answer.

[1 mark]

−2187 −128 2 128

2 Given that $y = 2x^3$ find $\frac{dy}{dx}$

Circle your answer.

[1 mark]

$\frac{dy}{dx} = 5x^2$ $\frac{dy}{dx} = 6x^2$ $\frac{dy}{dx} = \frac{x^4}{2}$ $\frac{dy}{dx} = 6x^3$



- 3** The curve with equation $y = \ln x$ is transformed by a stretch parallel to the x -axis with scale factor 2

Find the equation of the transformed curve.

Circle your answer.

[1 mark]

$$y = \frac{1}{2} \ln x$$

$$y = 2 \ln x$$

$$y = \ln \frac{x}{2}$$

$$y = \ln 2x$$

- 4** Given that θ is a small angle, find an approximation for $\cos 2\theta$

Circle your answer.

[1 mark]

$$1 - \frac{\theta^2}{2}$$

$$2 - 2\theta^2$$

$$1 - 2\theta^2$$

$$1 - \theta^2$$

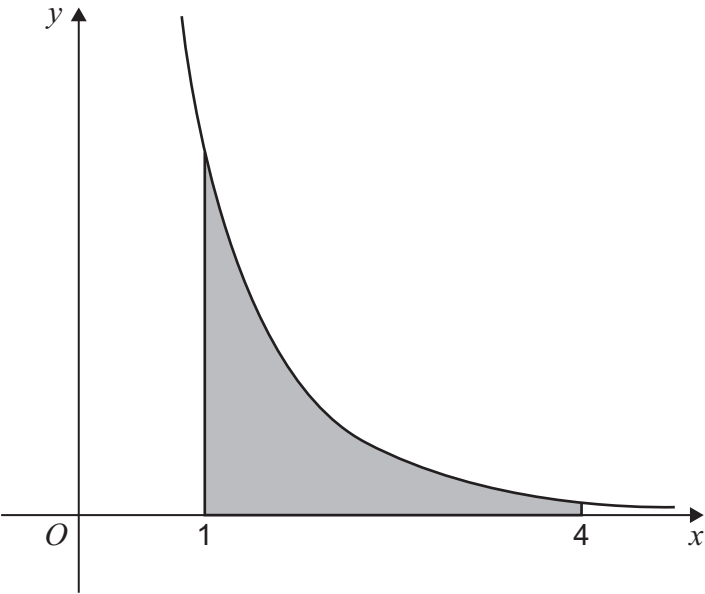
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5 The graph of $y = \frac{5}{e^x - 1}$ is shown in the diagram below.



The trapezium rule with 6 ordinates (5 strips) is to be used to find an approximation for the shaded area.

The values required to obtain this approximation are shown in the table below.

x	1	1.6	2.2	2.8	3.4	4
y	2.90988	1.26485	0.62305	0.32374	0.17263	0.09329

5 (a) Use the trapezium rule with 6 ordinates (5 strips) to find an approximate value for the shaded area.

Give your answer to four decimal places.

[3 marks]



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5 (b) Using your answer to part **(a)** deduce an estimate for $\int_1^4 \frac{20}{e^x - 1} \, dx$ **[1 mark]**

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7 (a) Given that n is a positive integer, express

$$\frac{7}{3 + 5\sqrt{n}} - \frac{7}{5\sqrt{n} - 3}$$

as a single fraction not involving surds.

[3 marks]

7 (b) Hence, deduce that

$$\frac{7}{3 + 5\sqrt{n}} - \frac{7}{5\sqrt{n} - 3}$$

is a rational number for all positive integer values of n

[1 mark]



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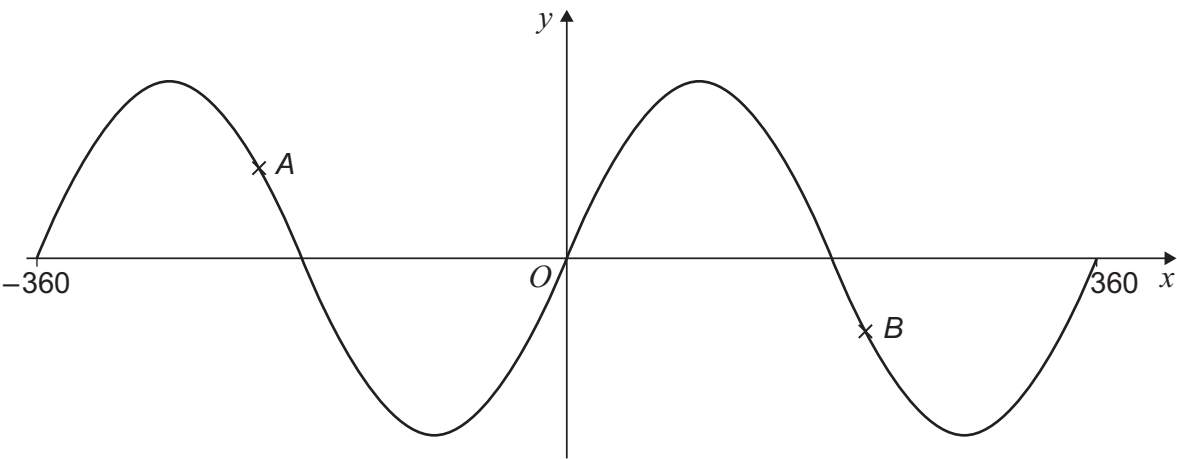


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10 The curve with equation

$$y = \sin x^\circ$$

for $-360 \leq x \leq 360$ is shown below.



10 (a) Point A on the curve has coordinates $(a, 0.5)$

10 (a) (i) Find the value of a

[2 marks]

10 (a) (ii) State the value of $\sin (180^\circ - a^\circ)$

[1 mark]



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10 (b) Point B on the curve has coordinates $\left(b, -\frac{3}{7}\right)$

10 (b) (i) Find the exact value of $\sin(b^\circ - 180^\circ)$ **[2 marks]**

10 (b) (ii) Find the exact value of $\cos b^\circ$ **[3 marks]**

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11 The n th term of a sequence is u_n

The sequence is defined by

$$u_{n+1} = pu_n + 70$$

where $u_1 = 400$ and p is a constant.

11 (a) Find an expression, in terms of p , for u_2

[1 mark]

11 (b) It is given that $u_3 = 382$

11 (b) (i) Show that p satisfies the equation

$$200p^2 + 35p - 156 = 0$$

[3 marks]



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11 (b) (ii) It is given that the sequence is a decreasing sequence.

Find the value of u_4 and the value of u_5

[3 marks]

11 (c) The limit of u_n as n tends to infinity is L

11 (c) (i) Write down an equation for L

[1 mark]

11 (c) (ii) Find the value of L

[1 mark]

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12 One of the rides at a theme park is a room where the floor and ceiling both move up and down for 10π seconds.

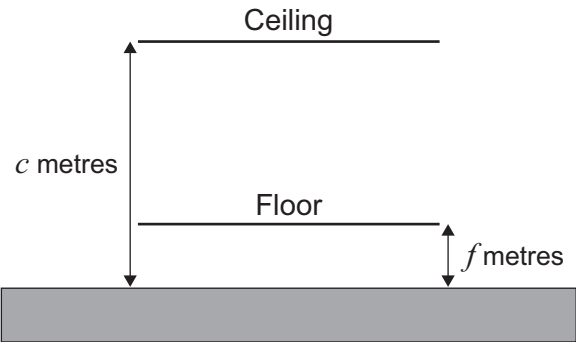
At time t seconds after the ride begins, the distance f metres of the floor above the ground is

$$f = 1 - \cos t$$

At time t seconds after the ride begins, the distance c metres of the ceiling above the ground is

$$c = 8 - 4 \sin t$$

The ride is shown in the diagram below.



12 (a) Show that the initial distance between the floor and ceiling is 8 metres.

[1 mark]



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12 (b) Show that the distance d metres between the floor and ceiling at time t is given by

$$d = 7 + R \cos(t + \alpha)$$

where R and α are positive constants to be found.

[5 marks]

12 (c) Hence, find the minimum distance between the ceiling and the floor.

Give your answer to the nearest centimetre.

[2 marks]

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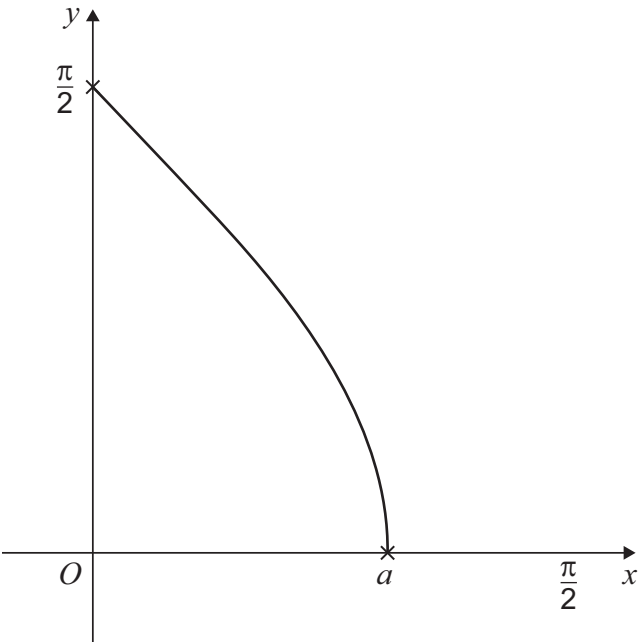


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13 The function f is defined by

$$f(x) = \arccos x \text{ for } 0 \leq x \leq a$$

The curve with equation $y = f(x)$ is shown below.



13 (a) State the value of a

[1 mark]

13 (b) (i) On the diagram above, sketch the curve with equation

$$y = \cos x \text{ for } 0 \leq x \leq \frac{\pi}{2}$$

and

sketch the line with equation

$$y = x \text{ for } 0 \leq x \leq \frac{\pi}{2}$$

[4 marks]



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13 (b) (ii) Explain why the solution to the equation

$$x - \cos x = 0$$

must also be a solution to the equation

$$\cos x = \arccos x$$

[1 mark]

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14 (a) (i) Given that

$$y = 2^x$$

write down $\frac{dy}{dx}$

[1 mark]

14 (a) (ii) Hence find

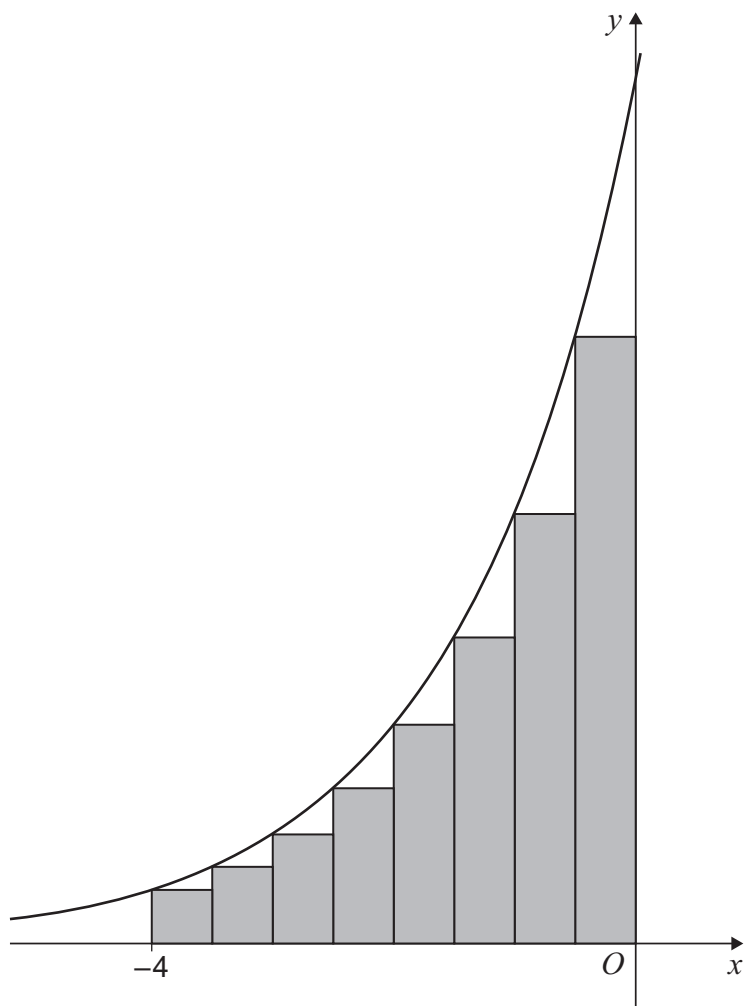
$$\int 2^x \, dx$$

[2 marks]



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- 14 (b)** The area, A , bounded by the curve with equation $y = 2^x$, the x -axis, the y -axis and the line $x = -4$ is approximated using eight rectangles of equal width as shown in the diagram below.



- 14 (b) (i)** Show that the exact area of the largest rectangle is $\frac{\sqrt{2}}{4}$ [2 marks]

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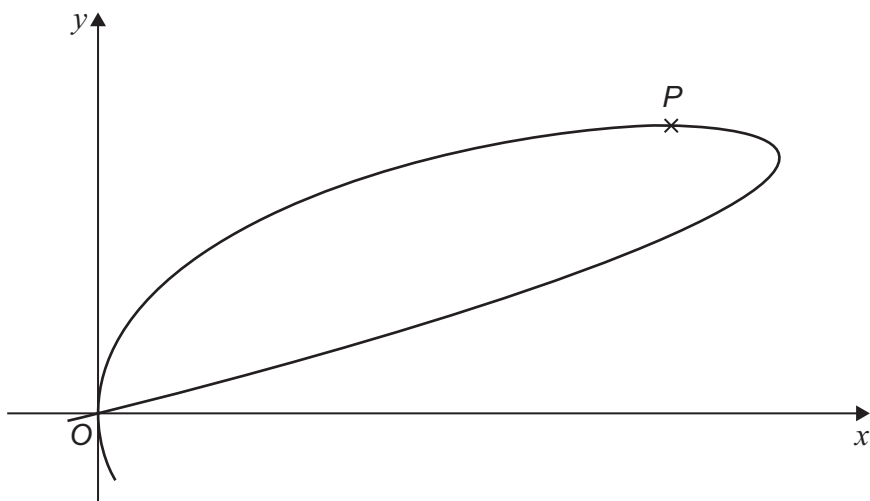
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15 The curve with equation

$$x^2 + 2y^3 - 4xy = 0$$

has a single stationary point at P as shown in the diagram below.



15 (a) Show that the y -coordinate of P satisfies the equation

$$y^2(y - 2) = 0$$

[7 marks]

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15 (b)

Hence, find the coordinates of P

[2 marks]

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16 (a) Given that

$$\frac{1}{16 - 9x^2} \equiv \frac{A}{4 - 3x} + \frac{B}{4 + 3x}$$

find the values of A and B

[3 marks]



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16 (b) (ii) Hence, find t in terms of V

[5 marks]

16 (b) (iii) Determine how long it takes to fill the container with water.

Give your answer to the nearest minute.

[2 marks]

END OF QUESTIONS



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