



Please write clearly in block capitals.

Centre number

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Candidate number

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Surname

Forename(s)

Candidate signature

I declare this is my own work.

AS FURTHER MATHEMATICS

Paper 1

Time allowed: 1 hour 30 minutes

Materials

- You must have the AQA Formulae and statistical tables booklet for A-level Mathematics and A-level Further Mathematics.
- You should have a scientific calculator that meets the requirements of the specification.

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer each question in the space provided for that question. If you require extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do **not** write outside the box around each page or on blank pages.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.

For Examiner's Use	
Question	Mark
1	
2	
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12	
13	
14	
15	
TOTAL	



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Answer **all** questions in the spaces provided.

- 1** Which of the following exponential expressions is equivalent to $2 \sinh x$?

Circle your answer.

[1 mark]

e^x $e^x + e^{-x}$ $e^x - e^{-x}$ e^{-x}

- 2** The quadratic equation $x^2 + px + q = 0$ has roots α and β

Which of the following is equal to $\alpha\beta$?

Circle your answer.

[1 mark]

p $-p$ q $-q$

- 3** Which of the following transformations is represented by the matrix $\begin{bmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$?

Tick (✓) **one** box.

[1 mark]

Rotation of 180° about the x -axis

Reflection in the plane $x = 0$

Rotation of 180° about the y -axis

Reflection in the plane $y = 0$



4 The complex numbers w and z are defined as

$$w = 2(\cos \alpha + i \sin \alpha)$$

$$z = 3(\cos \beta + i \sin \beta)$$

Find the product wz

Tick (✓) **one** box.

[1 mark]

$$5(\cos(\alpha\beta) + i \sin(\alpha\beta))$$

$$6(\cos(\alpha\beta) + i \sin(\alpha\beta))$$

$$5(\cos(\alpha + \beta) + i \sin(\alpha + \beta))$$

$$6(\cos(\alpha + \beta) + i \sin(\alpha + \beta))$$

Turn over for the next question

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6 The matrix **A** is given by

$$\mathbf{A} = \begin{bmatrix} 5 & 2 \\ -3 & 4 \end{bmatrix}$$

6 (a) Find $\det \mathbf{A}$

[1 mark]

6 (b) Find \mathbf{A}^{-1}

[1 mark]



7 The lines l_1 and l_2 have equations

$$l_1 : \mathbf{r} = \begin{bmatrix} 3 \\ 1 \\ -2 \end{bmatrix} + \lambda \begin{bmatrix} 3 \\ -4 \\ 1 \end{bmatrix}$$

$$l_2 : \mathbf{r} = \begin{bmatrix} -12 \\ a \\ -3 \end{bmatrix} + \mu \begin{bmatrix} 3 \\ 2 \\ -1 \end{bmatrix}$$

7 (a) Show that the point $P(-3, 9, -4)$ lies on l_1

[2 marks]

7 (b) Show that l_1 is perpendicular to l_2

[2 marks]



9 (a) Show that, for $r > 0$,

$$\ln(r + 2) - \ln r = \ln\left(1 + \frac{2}{r}\right)$$

[1 mark]

9 (b) Hence, using the method of differences, show that

$$\sum_{r=1}^n \ln\left(1 + \frac{2}{r}\right) = \ln\left(\frac{1}{2}(n + a)(n + b)\right)$$

where a and b are integers to be found.

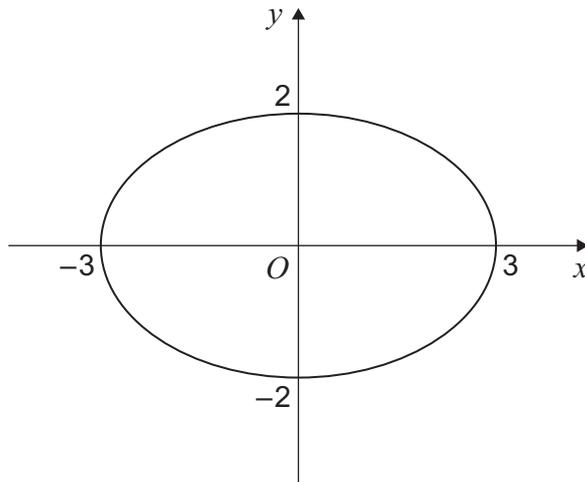
[4 marks]



10

The diagram below shows an ellipse E

The coordinate axes are the lines of symmetry of E



10 (a)

Write down an equation of E

[2 marks]



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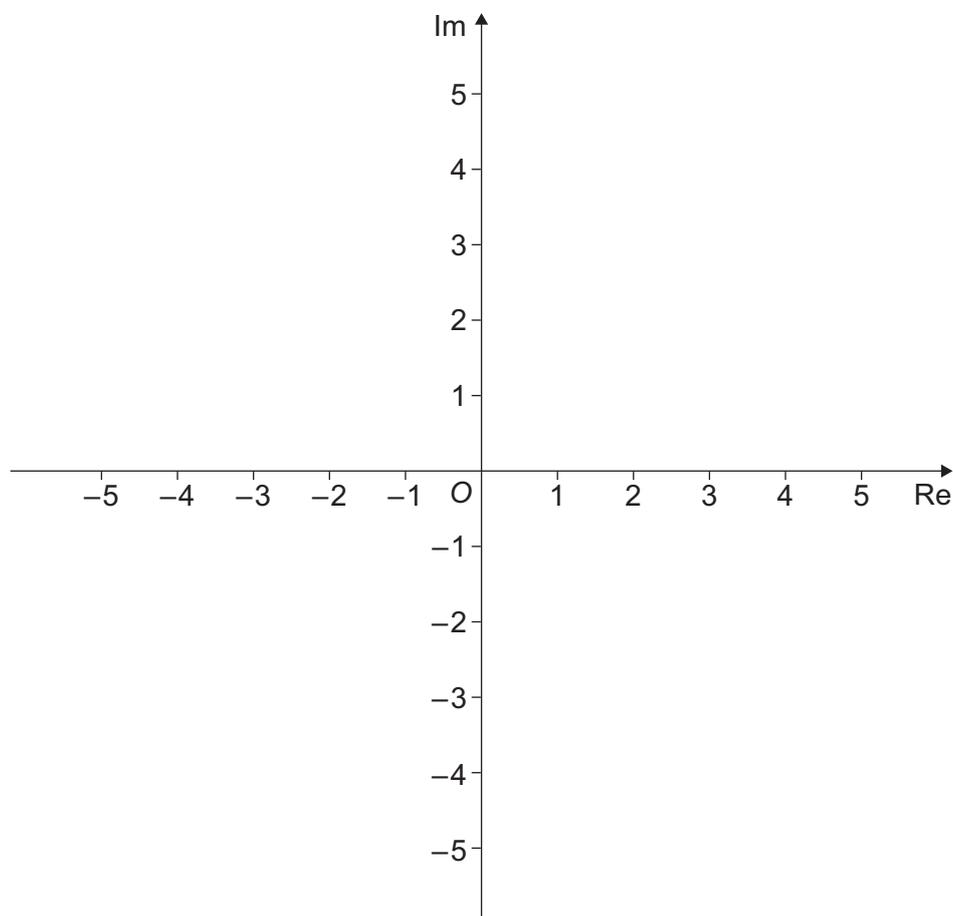
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12 (a) Sketch, on the Argand diagram below, the locus of points satisfying the equation

$$|z - 2i| = 2$$

[2 marks]



12 (b) Sketch, also on the Argand diagram above, the locus of points satisfying the equation

$$\arg z = \frac{\pi}{3}$$

[1 mark]



13 A curve C_1 has equation

$$y = \frac{2x + 7}{3x + 5}$$

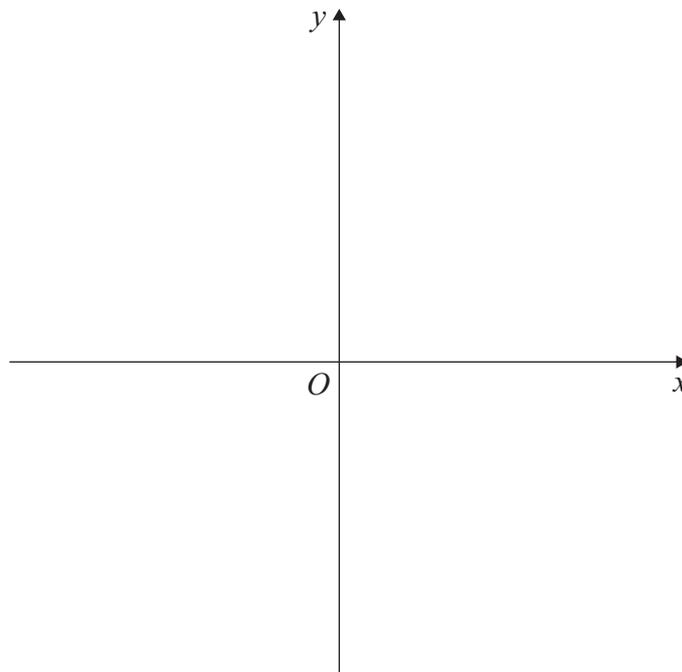
13 (a) Write down the equations of the asymptotes of curve C_1

[2 marks]

13 (b) On the axes below, sketch the graph of curve C_1

Indicate the values of the intercepts of the curve with the axes.

[3 marks]



13 (c) Hence, or otherwise, solve the inequality

$$\frac{2x + 7}{3x + 5} \geq 0$$

[2 marks]



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14 (c)

Find the coordinates of the points at which the graph of $y = f(x)$ intersects the axes.

[3 marks]

Question 14 continues on the next page

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14 (d) (ii) Hence, find the y -coordinate of point M

[2 marks]

Turn over for the next question

Turn over ►



15 The two values of θ that satisfy the equation

$$\sinh^2 \theta - \sinh \theta - 2 = 0$$

are θ_1 and θ_2

15 (a) Hamzah is asked to find the value of $\theta_1 + \theta_2$

He writes his answer as follows:

The quadratic coefficients are $a = 1$, $b = -1$, $c = -2$

The sum of the roots is $-\frac{b}{a}$

$$\text{So } \theta_1 + \theta_2 = -\frac{-1}{1} = 1$$

Explain Hamzah's error.

[1 mark]



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