Oxford Cambridge and RSA

GCE

Further Mathematics B MEI

Y412/01: Statistics A

AS Level

Mark Scheme for June 2022

OCR (Oxford Cambridge and RSA) is a leading UK awarding body, providing a wide range of qualifications to meet the needs of candidates of all ages and abilities. OCR qualifications include AS/A Levels, Diplomas, GCSEs, Cambridge Nationals, Cambridge Technicals, Functional Skills, Key Skills, Entry Level qualifications, NVQs and vocational qualifications in areas such as IT, business, languages, teaching/training, administration and secretarial skills.

It is also responsible for developing new specifications to meet national requirements and the needs of students and teachers. OCR is a not-for-profit organisation; any surplus made is invested back into the establishment to help towards the development of qualifications and support, which keep pace with the changing needs of today's society.

This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

Text Instructions

1 Annotations and abbreviations

Annotation in scoris	Meaning
✓and ✗	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
E	Explanation mark 1
SC	Special case
^	Omission sign
MR	Misread
BP	Blank page
Highlighting	
Other abbreviations in mark scheme	**Meaning**
E1	Mark for explaining a result or establishing a given result
dep*	Mark dependent on a previous mark, indicated by *. The * may be omitted if only previous M mark.
cao	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working
AG	Answer given
awrt	Anything which rounds to
BC	By Calculator
DR	This indicates that the instruction **In this question you must show detailed reasoning** appears in the question.

2. Subject-specific Marking Instructions for AS Level Mathematics B (MEI)

a Annotations must be used during your marking. For a response awarded zero (or full) marks a single appropriate annotation (cross, tick, M0 or ^) is sufficient, but not required.

For responses that are not awarded either 0 or full marks, you must make it clear how you have arrived at the mark you have awarded and all responses must have enough annotation for a reviewer to decide if the mark awarded is correct without having to mark it independently.

It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

Award NR (No Response)

- if there is nothing written at all in the answer space and no attempt elsewhere in the script
- OR if there is a comment which does not in any way relate to the question (e.g. 'can't do', 'don't know')
- OR if there is a mark (e.g. a dash, a question mark, a picture) which isn't an attempt at the question.

Note: Award 0 marks only for an attempt that earns no credit (including copying out the question).

If a candidate uses the answer space for one question to answer another, for example using the space for 8(b) to answer 8(a), then give benefit of doubt unless it is ambiguous for which part it is intended.

b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not always be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.
If you are in any doubt whatsoever you should contact your Team Leader.

c The following types of marks are available.

M
A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.
A method mark may usually be implied by a correct answer unless the question includes the DR statement, the command words "Determine" or "Show that", or some other indication that the method must be given explicitly.

A
Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

B
Mark for a correct result or statement independent of Method marks.

E
A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

d When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.

e The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only – differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case, please escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.
Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such

cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

f Unless units are specifically requested, there is no penalty for wrong or missing units as long as the answer is numerically correct and expressed either in SI or in the units of the question. (e.g. lengths will be assumed to be in metres unless in a particular question all the lengths are in km, when this would be assumed to be the unspecified unit.)
We are usually quite flexible about the accuracy to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so.

- When a value is **given** in the paper only accept an answer correct to at least as many significant figures as the given value.
- When a value is **not given** in the paper accept any answer that agrees with the correct value to **2 s.f.** unless a different level of accuracy has been asked for in the question, or the mark scheme specifies an acceptable range.
  NB for Specification A the rubric specifies 3 s.f. as standard, so this statement reads "3 s.f"

Follow through should be used so that only one mark in any question is lost for each distinct accuracy error.
Candidates using a value of 9.80, 9.81 or 10 for *g* should usually be penalised for any final accuracy marks which do not agree to the value found with 9.8 which is given in the rubric.

g Rules for replaced work and multiple attempts:

- If one attempt is clearly indicated as the one to mark, or only one is left uncrossed out, then mark that attempt and ignore the others.
- If more than one attempt is left not crossed out, then mark the last attempt unless it only repeats part of the first attempt or is substantially less complete.
- if a candidate crosses out all of their attempts, the assessor should attempt to mark the crossed out answer(s) as above and award marks appropriately.

h For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A or B mark in the question. Marks designated as cao may be awarded as long as there are no other errors. If a candidate corrects the misread in a later part, do not continue to follow through. E marks are lost unless, by chance, the given results are established by equivalent working. Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

i If a calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers provided that there is nothing in the wording of the question specifying that analytical methods are required such as the bold "In this question you must show detailed reasoning", or the command words "Show" and "Determine. Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.

j If in any case the scheme operates with considerable unfairness consult your Team Leader.

Question			Answer	Marks	AOs	
1	(a)		r: 1, 2, 3, 4, 5 P($X = r$): **$9k$**, $7k$, **$5k$**, $3k$, **k**	**B1** **[1]**	**1.1**	
1	(b)		$9k + 7k + 5k + 3k + k = 1 \Rightarrow k = \frac{1}{25}$ o.e.	**B1** **[1]**	**2.2a**	
1	(c)		E(X) $= \frac{11}{5}$ (= 2.2) Var(X) $= \frac{34}{25}$ (=1.36)	**B1** **B1** **[2]**	**1.1a** **1.1**	**BC** FT 55×their k **BC** FT 155×their k – their [E(X)]^2 provided Var(X) > 0
1	(d)		E(Winnings) = 50 × 2.2 = 110 C = 110 + 25 = 135	**M1** **A1** **[2]**	**1.1** **1.1**	FT 50 × their E(X) for M1 soi FT their E(X) Condone £1.35 and 135p
2	(a)		**Breakdowns** occur **randomly, independently** and at a **uniform average rate**	**E1** **E1** **[2]**	**3.3** **3.3**	Allow 'constant average rate'
2	(b)	(i)	P(exactly 4) = 0.0636	**B1** **[1]**	**1.1**	**BC** awrt 0.0636. Allow 0.064
2	(b)	(ii)	P(at least 2) = 1 – 0.4932 = 0.5068	**M1** **A1** **[2]**	**1.1a** **1.1**	**BC** M1 for attempt to find 1 – P(X < 2) **A**llow awrt 0.507, 0.51
2	(c)		Mean = 52 × 1.7 (= 88.4) P(less than 100) = 0.8799	**M1** **A1** **[2]**	**1.1** **1.1**	**BC** Allow 0.880, 0.88

Question			Answer	Marks	AOs	
3	(a)		Because the scatter diagram does not appear to be elliptical (but instead a curve) so the **distribution** is probably **not bivariate Normal**.	**E1*** **E1dep*** **[2]**	**3.5b** **3.5b**	For not elliptical For full answer (dependent on first mark) If no E marks awarded SC B1 for the association might not be linear.
3	(b)		<table><tr><td>Rank PC</td><td>1</td><td>3</td><td>2</td><td>4</td><td>6</td><td>5</td><td>8</td><td>10</td><td>7</td><td>9</td></tr><tr><td>Rank DW</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr></table> Spearman's rank coefficient = 0.9152 $\left(=\frac{151}{165}\right)$	**M1** **M1** **A1** **[3]**	**1.1** **1.1** **1.1**	For ranking DW For ranking PC. Allow both ranks reversed **BC** Allow 0.915, 0.92
3	(c)		**H_0**: There is **no association** between percentage colonisation and shoot dry weight in the population **H_1**: There is **some association** between percentage colonisation and shoot dry weight in the population (For $n = 10$, 2-tailed 5% critical value is) 0.6485 0.9152 > 0.6485 (Reject H_0) There is evidence to **suggest** that there is association between percentage colonisation and shoot dry weight in the population.	**B1** **B1** **B1** **M1** **A1** **[5]**	**2.5** **1.2** **3.4** **1.1** **2.2b**	For hypotheses in context For population seen in either of the hypotheses Allow 0.649 For correct comparison of their r_s with their critical value provided $\lvert r_s\rvert < 1$ For correct non-assertive conclusion in context. FT their r_s but A0 if wrong critical value used.

4	(a)		(Discrete) **Uniform (**distribution). (On the values) {1, 2, …, 50}	**B1*** **B1dep*** **[2]**	**3.3** **1.2**	For uniform For values SC B1 if 'uniform' is not stated but correct probability distribution is seen
4	(b)		E(X) = 25.5 Var(X) = 208.25 (s.d. = 14.4 oe) Need ($11.1 < X < 39.9$) $12 \le X \le 39$ $=\frac{28}{50} = 0.56$	**B1** **B1** **M1** **A1** **[4]**	**1.1a** **1.1** **3.1a** **1.1**	For correct variance or standard deviation For finding their E(X) ± their s.d., giving appropriate integer bounds. cao www

Question			Answer	Marks	AOs	
5	(a)		The sample must be **random**	**B1** [1]	**1.2**	
5	(b)		C11: 8.70 C18: $\frac{(10-10.15)^2}{10.15}$ = 0.0022	**B1** **M1** **A1** [3]	**1.1** **1.1** **1.1**	Allow 8.7 cao Answer correct to 4 d.p.
5	(c)		H_0: No association between A-Level Mathematics grade and GCSE performance H_1: Some association between A-Level Mathematics grade and GCSE performance Degrees of freedom = 4 Test statistic = 2.1680 + 0.8002 + ... + 2.2857 = 8.9721 Critical value = 7.779 8.972 > 7.779 so reject H_0 There is evidence (at the 10% level) to **suggest** that there is association between A-Level Mathematics grade and GCSE performance	**B1** **B1** **B1** **M1** **A1** [6]	**3.4** **3.3** **1.1** **1.1** **2.2b** **3.5a**	Allow H_0: 'A-Level Mathematics grade and GCSE performance are independent' H_1: 'A-Level Mathematics grade and GCSE performance are not independent' Allow 8.972, 8.97 FT their C18 Or $\chi^2_4(8.97) = 0.938$ For correct comparison of their test statistic with their critical value leading to consistent conclusion Or 0.938 > 0.90 so reject H_0 FT their test statistic but A0 if wrong critical value used or if hypotheses reversed
5	(d)		For **Low** performance the high contribution (of 2.1680) suggests **fewer get A* or A than** would be **expected** (if there were no association). For **Middle** performance the low contributions suggest that **things are as** would be **expected** (if there were no association). For **High** performance the high contributions (of 1.5873 and 2.2857) suggest that **more than expected get A* or A and that fewer than expected get C or lower** (than would be expected if there were no association).	**E1** **E1** **E1** [3]	**2.2b** **3.5a** **3.5a**	If contributions not mentioned then award max SC B1 B1 for interpretations that are otherwise correct.
5	(e)		The null hypothesis is more likely to be wrongly rejected	**E1** [1]	**2.2a**	The alternative hypothesis is more likely to be wrongly accepted. Or there is a greater chance of a false positive.

Question			Answer	Marks	AOs	Guidance	
6	(a)		$S_{xy} = 5009.1 - \frac{1}{8} \times 268 \times 141.9 = 255.45$ $S_{xx} = 9618 - \frac{1}{8} \times 268^2 = 640$ $b = \frac{255.45}{640} = 0.3991\ldots$ $a = \frac{141.9}{8} - 0.3991\ldots \times \frac{268}{8} = 4.3662\ldots$ $y = 0.399x + 4.37$	M1 A1 M1 A1 [4]	1.1a 1.1 1.1 1.1	For correct substitution into S_{xy} or S_{xx} For b For method for a. FT their b and means. cwo Allow final mark only if equation explicitly stated. Awrt 0.399 and 4.37 in final answer.	
6	(b)		Prediction for x = 35 is y = 18.3 Prediction for x = 10 is y = 8.4	B1 B1 [2]	1.1 1.1	Allow 18.34. FT their final equation if correct substitution seen and given as a decimal correct to no more than 2 d.p. Allow 8.36. FT their final equation if correct substitution seen and given as a decimal correct to no more than 2 d.p. SCB1 if B0B0 awarded due to over-specification	
6	(c)		e.g. The prediction for x = 35 is likely to be fairly reliable since this is **interpolation** and the points appear to follow a linear trend. The prediction for x = 10 is less likely to be reliable since this is **extrapolation**, well below any data values.	B1 E1 B1 [3]	2.2b 2.2b 3.5a	Must have some element of doubt to get 2 marks for prediction for x = 35	
6	(d)		Coordinates are (33.5, 17.7(375))	B1 [1]	1.1		

Question			Answer	Marks	AOs	Guidance	
7	(a)		Geometric(0.2)	**M1** **A1** **[2]**	**3.3** **1.1**	M1 for distribution. Allow Geo(…) for parameter	
7	(b)		$0.8^3 \times 0.2 = 0.1024$	**B1** **[1]**	**1.1**	**BC** Allow 0.102	
7	(c)		Must find 1 voucher in first 9 so B(9, 0.2) then × 0.2 P(second on tenth) = $9 \times 0.8^8 \times 0.2 \times 0.2$ $= 0.060$ (0.060397…)	**M1** **A1** **[2]**	**1.1** **1.1**	**BC** Or 0.30198… × 0.2	
7	(d)		$1-0.8^n > 0.99 \Rightarrow 0.8^n < 0.01$ $n > \frac{\ln 0.01}{\ln 0.8}$ so least $n = 21$	**M1** **A1** **[2]**	**3.1b** **3.2a**	M1 for $0.8^n < 0.01$ A1 for $n = 21$ www. SC B1 for n = 21 from $0.8^n \leq 0.01$ or $0.8^n = 0.01$ If trial and improvement used award M1 if suitable inequality shown and A1 for n = 21 with suitable working shown. SC B1 for n = 21 if inequality not shown but suitable probabilities seen. e.g. $P(X \leq 20) = 0.9884..$ and $P(X \leq 21) = 0.9907..$	

Need to get in touch?

If you ever have any questions about OCR qualifications or services (including administration, logistics and teaching) please feel free to get in touch with our customer support centre.

Call us on

01223 553998

Alternatively, you can email us on

support@ocr.org.uk

For more information visit

ocr.org.uk/qualifications/resource-finder

ocr.org.uk

Twitter/ocrexams

/ocrexams

/company/ocr

/ocrexams

CAMBRIDGE
UNIVERSITY PRESS & ASSESSMENT

OCR is part of Cambridge University Press & Assessment, a department of the University of Cambridge.

OCR operates academic and vocational qualifications regulated by Ofqual, Qualifications Wales and CCEA as listed in their qualifications registers including A Levels, GCSEs, Cambridge Technicals and Cambridge Nationals.

OCR provides resources to help you deliver our qualifications. These resources do not represent any particular teaching method we expect you to use. We update our resources regularly and aim to make sure content is accurate but please check the OCR website so that you have the most up-to-date version. OCR cannot be held responsible for any errors or omissions in these resources.

Though we make every effort to check our resources, there may be contradictions between published support and the specification, so it is important that you always use information in the latest specification. We indicate any specification changes within the document itself, change the version number and provide a summary of the changes. If you do notice a discrepancy between the specification and a resource, please contact us.

Whether you already offer OCR qualifications, are new to OCR or are thinking about switching, you can request more information using our Expression of Interest form.

Please get in touch if you want to discuss the accessibility of resources we offer to support you in delivering our qualifications.