

# **GCE**

**Further Mathematics A** 

Y542/01: Statistics

A Level

Mark Scheme for June 2022

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All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

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## **Text Instructions**

## 1. Annotations and abbreviations

Annotation in RM assessor	Meaning
√and <b>x</b>	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
۸	Omission sign
MR	Misread
BP	Blank Page
Seen	
Highlighting	
Other abbreviations in	Meaning
mark scheme	
dep*	Mark dependent on a previous mark, indicated by *. The * may be omitted if only one previous M mark
cao	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working
AG	Answer given
awrt	Anything which rounds to
BC	By Calculator
DR	This question included the instruction: In this question you must show detailed reasoning.

### 2. Subject-specific Marking Instructions for A Level Mathematics A

a Annotations must be used during your marking. For a response awarded zero (or full) marks a single appropriate annotation (cross, tick, M0 or ^) is sufficient, but not required.

For responses that are not awarded either 0 or full marks, you must make it clear how you have arrived at the mark you have awarded and all responses must have enough annotation for a reviewer to decide if the mark awarded is correct without having to mark it independently.

It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

Award NR (No Response)

- if there is nothing written at all in the answer space and no attempt elsewhere in the script
- OR if there is a comment which does not in any way relate to the question (e.g. 'can't do', 'don't know')
- OR if there is a mark (e.g. a dash, a question mark, a picture) which isn't an attempt at the question.

Note: Award 0 marks only for an attempt that earns no credit (including copying out the question).

If a candidate uses the answer space for one question to answer another, for example using the space for 8(b) to answer 8(a), then give benefit of doubt unless it is ambiguous for which part it is intended.

An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not always be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.

If you are in any doubt whatsoever you should contact your Team Leader.

c The following types of marks are available.

#### М

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

A method mark may usually be implied by a correct answer unless the question includes the DR statement, the command words "Determine" or "Show that", or some other indication that the method must be given explicitly.

### Α

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

### В

Mark for a correct result or statement independent of Method marks.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep\*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case please, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.
  - Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.
- f We are usually quite flexible about the accuracy to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so.
  - When a value is given in the paper only accept an answer correct to at least as many significant figures as the given value.
  - When a value **is not given** in the paper accept any answer that agrees with the correct value to **3 s.f.** unless a different level of accuracy has been asked for in the question, or the mark scheme specifies an acceptable range.

Follow through should be used so that only one mark in any question is lost for each distinct accuracy error.

Candidates using a value of 9.80, 9.81 or 10 for *g* should usually be penalised for any final accuracy marks which do not agree to the value found with 9.8 which is given in the rubric.

- g Rules for replaced work and multiple attempts:
  - If one attempt is clearly indicated as the one to mark, or only one is left uncrossed out, then mark that attempt and ignore the others.
  - If more than one attempt is left not crossed out, then mark the last attempt unless it only repeats part of the first attempt or is substantially less complete.
  - if a candidate crosses out all of their attempts, the assessor should attempt to mark the crossed out answer(s) as above and award marks appropriately.
- For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A or B mark in the question. Marks designated as cao may be awarded as long as there are no other errors. If a candidate corrects the misread in a later part, do not continue to follow through. Note that a miscopy of the candidate's own working is not a misread but an accuracy error.
- If a calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers, provided that there is nothing in the wording of the question specifying that analytical methods are required such as the bold "In this question you must show detailed reasoning", or the command words "Show" or "Determine". Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.
- j If in any case the scheme operates with considerable unfairness consult your Team Leader.

	Question		Answer	Marks	AO	Guidance	
1	(a)	(i)	Geo(0.01)	B1	1.1	Allow if 0.01 not stated here but used in (ii)	
	(a)	(ii)	$q^m - q^n$ where $m = 50, 49, 51, n = 150, 149, 151$	M1	2.1	e.g. 0.378, 0.386, 0.387, 0.381, 0.390, 0.392. Their q	Or $pq^{50} + + pq^{149} = pq^{50}(1 - q^{100})/(1 - q)$
			$q^{50} - q^{150} = 0.384 (0.38355)$	<b>A1</b>	1.1	In range [0.383, 0.384], cao	± 1 term at either end for M1
							M1 needs method for summing GP
	<b>(b)</b>		$E(R) = 1/p$ and correct $Var(R) = (1-p)/p^2$	M1	1.1	Art least one correct general formulae stated	
			$= (1/p)^2 - (1/p) = [E(R)]^2 - E(R)$	A1	2.1	Correctly show required relationship, either way	
				[2]		round, don't need conclusion, not numerical	
2	(a)		Independent (and no others)	B1	2.5	Fully correct only	
	(b)		0.713 BC	B2	1.1	SC: If B0, give B1 for any 2 of 16.02, 14.24,	
				[2]	1.1	10.77, or any 2 of 192.25, 170.9, 129.25 seen	e.g. 769/4, 2051/12, 517/4
	(c)	(i)	"More computer failures when	B1	2.4	Oe	
			temperatures are <u>higher</u> ", rather than	[1]		Allow "Looking for positive correlation", etc	
			"number of failures is related to higher <u>or</u>				
			<u>lower</u> temperatures"				
						Treat association and correlation as equivalent	See Appendix for exemplars
	(c)	(ii)	$H_{0:} \rho = 0, H_1: \rho > 0$	B2	1.1	One error, e.g. 2-tail, or $\rho$ not defined: B1	Verbal, e.g. H <sub>0</sub> : no correlation between
			where $\rho$ is the population PMCC between		2.5	(allow H <sub>0</sub> : $\rho \le 0$ ). Allow omission of "population"	temperature and number of failures, H <sub>1</sub> :
			temperature and number of failures			(or "true") or of context, but not of both	positive correlation: max B1, one error B0
			CV = 0.6581	B1	1.1	Correct CV, $or p = 0.00462$	
			0.713 > 0.6581	B1ft	1.1	Explicit comparison, their $r$ , allow "pmcc $> CV$ "	Their CV must be from tables for $r$ or $r_s$
			Reject H <sub>0</sub> . Significant evidence of	M1ft	1.1	FT on their <i>r</i> , needs 0.6581, 0.6851, 0.7079,	If inconsistent with comparison, M0A0
			(positive) correlation between temperature	A1ft	2.2b	0.4973 or 0.5760; contextualised, not too definite	Not "insufficient evidence of no correlation
	(1)		and number of failures	[6]	1.0	TOTAL 1 (1) A 11 (4) 1 199 (	between"
	(d)		0.713	B1ft [1]	1.2	Their (b). Allow "unchanged", etc.	
3			<b>DR</b> $E(V) = q + 0.24 + 0.6$	B1	3.1a		
			$E(V^2) = q + 0.48 + 1.8$	B1	1.1		$Or: E(V - E(V))^2: M1$
			$q + 0.84 = q + 2.28 - (q + 0.84)^2$	M1	2.1	Use $E(V^2) - [E(V)]^2$	then eliminate p: M1
			$(q+0.84)^2=1.44$	A1	1.1	Correct simplified quad, eg $q^2 + 1.68q - 0.7344 = 0$	Or $625q^2 + 1050q - 459 = 0$
			so $q = -0.84 \pm 1.2$	M1	1.1	Solve quadratic, valid method seen or implied	Can be implied by one correct root
			Reject $q = -2.04$ as negative	B1	2.3	Explicitly reject invalid solution, with reason	Or reason to take + root of 1.44
			q = 0.36	<b>A1</b>	2.2a	0.36 or exact equivalent seen, e.g. 9/25	
			p = 1 - 0.32 - q = 0.32	B1ft	1.1	p = 0.68 – their q. Withhold if extra solutions seen	E.g. 8/25
				[8]		SC: $E(V^2) - E(V)$ : (B1B1) $q = 0.6$ B1, $p = 0.08$ B1	Use Poisson: 0/8

(	Questi	on	Answer	Marks	AO	Guidance	
4	(a)		Punctures must occur at constant average	B1	3.3	Constant average rate (or uniform rate), with	<i>Not</i> constant rate, <i>not</i> constant probability,
			rate throughout the period of 24 hours	[1]		context (not events must occur), no extras	not average constant rate, not singly
	<b>(b)</b>		$\sqrt{2.7} = 1.64(3)$	<b>B1</b>	1.1	Any equivalent answer, e.g. $3\sqrt{30/10}$	
4	(c)		Po(18.9)	M1	1.1	$Po(7\times2.7)$ stated or implied	
			$1 - P(\leq 21)$	M1	3.4	Probability from their $Po(7 \times 2.7)$	E.g. $1 - P(\le 22) = 0.2(0015) \text{ M1M1A0}$
			= 0.267	<b>A1</b>	1.1	Awrt 0.267	
	( <b>d</b> )		Po(3.5)	M1	1.1	Stated or implied, e.g. by $1 - 0.858 = 0.142$	
			P(>6) = 0.0653	A1	3.4	Correct calculation, awrt 0.0653	
	(e)		0.0653 is some way from 0.12	B1ft	3.5b	Compare 0.12 with answer to (d), or other	<i>Or:</i> B(100, 0.0653), P( $\geq$ 12) = 0.03 or
						appropriate calculation and comparison	E(R) = 6.5, etc
			so assumptions look doubtful (but possible	B1ft	3.5a	Appropriate assessment, not definite (and correct	See Appendix for exemplars
			as 100 days may not be enough evidence)	[2]		calculation, if used). FT on their (d)	
5	(a)		80 + 2X	M1	3.1b	Consider distribution of $80 + 2X$	OR: make X subject M1
			~ N(246,	M1	1.1	Normal with mean 246	$X < 77.5 \text{ (or } \le 77)$ A1
			1440)	A1	1.1	Correct variance	$P(X < 77.5)$ from N(83, 360) M1, allow $\le 77$
			P(<£235) = 0.386	A1	3.4	Awrt 0.386	P(<£235) = 0.386  A1  (0.376  A0)
				[4]			$Or P(2X < 155)$ where $2X \sim N(166, 1440)$
	<b>(b)</b>		Using costs $A_1$ , $A_2$ , $A_3$ , $B_1$ , $B_2$ :				If in effect using $3X$ , $2Y$ :
			$A_1 = 80 + 2X_1 \sim N(246, 1440)$	B1	1.1	Means 246, 244.5, can be implied by later work	Means 246, 244.5 B1
			$B_1 = 120 + 1.5X_4 \sim N(244.5, 810)$	B1	2.2a	Variances 1440, 810, ditto	Variances 1440, 810 B1
			$A_1 + A_2 + A_3 \sim N(738, 4320)$	B1 B1	1.1	Means 738 & 489, allow 498 & 249	Means 738, 489 B1 Variances 12960, 3240 B0
			$B_1 + B_2 \sim N(489, 1620)$	M1	1.1 3.1b	Variances 4320 and 1620 Use normal for difference, add variances	Variances 12960, 3240 B0 N(249, 16200) M1
			Difference ~ N(249, 5940) P(diff $\ge 300$ ) = 0.254	A1 [6]	3.10	Awrt 0.254, allow ±0.02 if cc used	0.344 A0
		OR	Using distances $X_1$ , $X_2$ , $X_3$ , $X_4$ , $X_5$ :	AI [U]	3.4	Awit 0.234, allow ±0.02 if cc used	If in effect using 3X, 2Y:
		OK	Using distances $X_1$ , $X_2$ , $X_3$ , $X_4$ , $X_5$ . $X_1 + X_2 + X_3 \sim N(249, 1080)$	B1		Means 249, 166, can be implied by later work	Means 249, 166 B1
			$X_1 + X_2 + X_3 \approx 14(249, 1000)$ $X_4 + X_5 \approx N(166, 720)$	B1		Variances 1080, 720, ditto	Variances 3240, 1440 B0
			A's charge $\sim N(738, 4320)$	B1		Means 738 & 249, allow 498 & 249	Means 738, 489 B1
			B's charge ~ N(489, 1620)	B1		Variances 4320 and 1620	Variances 12960, 3240 <b>B1 NB</b>
			Difference ~ N(249, 5940)	M1		Use normal for difference, add variances	N(249, 16200) M1
			$P(diff \ge 300) = 0.254$	A1		Awrt 0.254, allow $\pm 0.02$ if cc used	0.344 A0
		OR	Diff in costs is $2(X_1+X_2+X_3)-1.5(X_4+X_5)$	M1A1		M1 needs attempt to include constants	
			~ N(249, 5940)	M1A2		M1 N(249,), A2 variance correct, A1 for 16200	SC: variance formula seen correct but
			$P(diff \ge 300) = 0.254$	A1		Awrt 0.254, allow $\pm 0.02$ if cc used	wrongly calculated: (M1)M1 SCM1
			SC1: insufficient working shown			0.254 www gets 6/6; 0.746 www gets 5/6 [A0]	0.344 www gets 4/6 [A0A0]; all else 0/6
			SC2: assume all/both variables equal:	M1A1		3X > 300  M1 N(249, 3240) or N(±51, 3240) A1	Or N(83, 360) and compare 100: A1 (0.185)

	Question	Answer	Marks	AO	Guidance	
6	(a)	Mean 30.7	B1	1.1	Seen or implied	Inequalities can be omitted until final line
		Biased variance 22.225 (SD 4.714)	M1	1.1	Calculate variance, allow biased here	
		$22.225 \times 128/127 = 22.4$ (SD 4.733)	M1	1.2	×128/127 seen, or implied used	Independent of previous M1.
		$1 - \Phi((30.7 - 30)/\sqrt{(22.4/128)})$	M1	1.1	Standardise with 128, answer < 0.5 or 50%	E.g. 4.6% seen (from no 128/127). <i>Not</i> 0.441
		Range is $\ge 0.047 (\ge 4.7\%)$	A1	2.2a	Allow > or $\geq$ oe. Awrt 0.047 or 4.7%. CWO.	No 128/127, or wrong z: max 3/5
			[5]		Wrong or no range: A0. Allow = $4.71 \text{ so } \ge 5\%$	Insuff working: $4.7\% \Rightarrow 5/5, 4.6\% \Rightarrow 3/5$
					0.0464 is probably B1M1M0M1A0	0 with some evidence [( $\sqrt{22.4}$ )/128]: 4/5
6	(b)	128 large enough (for CLT to apply)	M1	2.3	Reason, e.g. sample is large, or $n > 25$	SC1: CLT applies so not invalidated: B1
		Hence test not invalidated	A1	2.3	Conclusion, allow "test is valid" or just "no"	SC2: CLT applies as $n >$ (any number other
			[2]		Wrong extras, eg "all dists approach normal": M0	than 25): max B1
7		$\int_0^1 kx^n dx = 1 \implies k = n + 1$	M1	2.1	Equate integral of $f(x)$ , upper limit 1, to 1	
		$J_0$ and $J_0$	A1	1.1	Correct equation for <i>n</i> and <i>k</i>	
		$\grave{\mathbf{O}}_0^{0.8816} kx^n \mathrm{d}x = 0.5$	M1*	1.1	Equate integral of $f(x)$ , upper limit 0.8816, to 0.5	
		$k(0.8816)^{n+1}/(n+1) = 0.5$ and use $k = n+1$	depM1	3.1a	Set up equation in <i>n</i> or <i>k</i> only	0.8816 and 0.5 reversed: (M1A1M1)
		$0.8816^{n+1} = 0.5$	A1	1.1	Correct equation [or $0.8816^k = 0.5$ ]	M1A0A0 (M1A1)
		n = 4.5  or  k = 5.5	<b>A1</b>	3.1a	Correct <i>n</i> or <i>k</i> , awrt $4.5(0)$ or $5.5(0)$	
		$P(X < 0.8) = 0.8^{5.5} (= 0.293)$	M1	3.4	Use their $\int f(x)$ , upper limit 0.8, with their $n$	
		E(number < 0.8) = 2.93	A1ft	2.2a	$10 \times (\text{their } p)$	Not just 3, but ISW if 2.93 rounded to 3
			[8]		NB: can get 2.93 from wrong integration	
8	(a)	$\mu = 264$	B1	3.1a	Allow even if no CC used	
		$^{1}/_{4}n(n+1) = 264$	M1	1.1	Use formula for mean	Or: $113 + 415 = \frac{1}{2}n(n+1)$ : M2
		$\Rightarrow$ $n = 32$ or $-33$ , but $n > 0$ so 32 only <b>AG</b>	A1 [3]	2.2a	Solve $n^2 + n - 1056 = 0$ to obtain 32	Can be implied by both 32 and –33 Just verification: SC B1
	(b)	Variance = $\frac{1}{24}n(n+1)(2n+1) = 2860$	B1	3.3	Variance 2860 stated or implied	
		$\Phi(113.5 - 264)/\sqrt{2860} \ (= 0.002445)$	M1*	3.4	Standardise, their parameters (or use 414.5)	No or wrong cc: (0.503% or 0.518%):
		$\Rightarrow r = 2 \times 0.002445 \times 100\%$	depM1	3.1b	Double their <i>p</i> -value ( $p < 0.5$ ), oe	B1M1M1A0
		= 0.489 (%)	A1	2.2a	0.49 or better (0.48 is probably from no cc)	Allow 0.50% <i>only</i> if correct CC seen
			[4]		or y or court (or to is procuerly from no co)	
9	(a)	H <sub>0</sub> : data consistent with belief, H <sub>1</sub> : not	B1	1.1	OE, e.g. "follows the given ratio"	
		Expected frequencies 30, 20, 20, 20, 30	B1	1.1	Stated or implied	
		$X^2$ values 0.1333, 0.8, 0.8, 0.8, 1.2	M1	3.4	At least two correct, or correct subs in formula	Can be implied by answer
		Total 3.73(333) $(=\frac{56}{15})$	A1	1.1	Fully correct	SC: Some cells merged:
		< 9.488	A1	1.1	Compare with 9.488, or $p = 0.443 > 0.05$	can get B2M1A0A0 M1A1
		Do not reject $H_0$ . Insufficient evidence that	M1ft	1.1	Consistent first conclusion, FT on their $X^2$	Needs CV 9.488 or 11.14 or 7.815
		data inconsistent with head's belief	A1ft	2.2b	Contextualised, not over-definite	Withhold A1 if hypotheses reversed
			[7]		Sufficient evidence that belief is correct: A0	Insuff evidence to reject H <sub>0</sub> , belief correct M1A1

Quest	ion	Answer	Marks	AO	Guidance	
(b)		"Determine", so needs proper working $3.73(333) \times n/120 > 9.488$ ( $\Rightarrow 7n/225 > 9.488$ ) $\Rightarrow n \ge 305 (3 \text{ sf})$ Must be multiple of 30, so least $n$ is 330	M1 A1 B1ft	3.1b 1.1 3.2a	Inequality for $n$ , using TS and CV $n > 305$ or $n \ge 305$ stated or implied, allow 306 Next multiple of 30 above <i>their</i> 305	3.73 gives 305.2, 3.733 gives 304.97 e.g. answer of 305 or 306 Needs reason if rounded up by < 10 or to
			[3]		r	multiple of 300
	OR	$\frac{\left(\frac{7n}{30} - \frac{3n}{12}\right)^2}{\frac{3n}{12}} + 3 \times \frac{\left(\frac{4n}{30} - \frac{2n}{12}\right)^2}{\frac{2n}{12}} + \frac{\left(\frac{9n}{30} - \frac{3n}{12}\right)^2}{\frac{3n}{12}}$ $= \frac{1}{900}n + 3 \times \frac{1}{150}n + \frac{1}{100}n > 9.488$	M1		Inequality for <i>n</i> , using 120, TS and CV, needs <i>n</i> in both O and E terms  ()	Or T& I: $n = 300 \rightarrow 9.333$ Any $n$ in range 300 to 360, with $\Sigma x^2$ in [9.33, 11.2]: M1 $n = 330 (9.489)$ A2 $(n = 305 \rightarrow 9.489)$ A1)
		$(\Rightarrow 7n/225 > 9.488) \Rightarrow n \ge 305 (3 \text{ sf})$	A1		$n > 305$ or $n \ge 305$ stated or implied, allow 306	e.g. answer of 305 or 306
		Must be multiple of 30, so least <i>n</i> is 330	B1ft		Next multiple of 30 above their 305, needs reason	Or <i>n</i> /120 must be a multiple of 0.25

### **APPENDIX**

## Exemplar responses for Q2(c)(ii)

### Hypotheses

Verbal statements

A	H <sub>0</sub> : no correlation between variables, H <sub>1</sub> : positive correlation between variables [no context]	B0			
В	H <sub>0</sub> : no correlation between number of failures and temperature, H <sub>1</sub> : correlation between number of failures and	В0			
	temperature [not one-tailed: needs "positive" in $H_1$ ]				
С	H <sub>0</sub> : no evidence of correlation between runners' positions, H <sub>1</sub> : evidence of positive correlation between number of	В0			
	failures and temperature ["evidence" does not belong in hypotheses; without "evidence of" ×2 this would be B1]				
States	Statements using parameter symbol [mark statements using r in place of a identically]				

Statements using parameter symbol [mark statements using r in place of  $\rho$  identically]

D	$H_0: \rho = 0, H_1: \rho \ge 0$ [two errors: $H_1$ wrong, no interpretation of $\rho$ ]	B0
Е	$H_0$ : $\rho = 0$ , $H_1$ : $\rho \neq 0$ [two errors: $H_1$ wrong, no interpretation of $\rho$ ]	В0
F	$H_0$ : $r = 0$ , $H_1$ : $r > 0$ [one error: no interpretation of $\rho$ . Allow use of $r$ ]	B1
G	$H_0$ : $\rho = 0$ , there is no correlation between number of failures and temperature; $H_1$ : $\rho > 0$ , there is positive correlation	B1
	[two different answers, either of which would score 1 but neither gains 2 and we don't give 1+1 here]	
Н	$H_0$ : $\rho = 0$ , $H_1$ : $\rho > 0$ , where $\rho$ is the pmcc [neither "population" nor context]	B1
I	$H_0$ : $\rho \le 0$ , $H_1$ : $\rho > 0$ , where $\rho$ is the population pmcc	B2
	$OR H_0$ : $\rho = 0$ , $H_1$ : $\rho > 0$ , where $\rho$ is the pmcc between temperature and number of failures	

**Conclusions** (In general, allow "Accept  $H_0$ " as a synonym for "Do not reject  $H_0$ ", etc.)

A	Reject H <sub>0</sub> . There are more computer failures when temperatures are higher [too definite]	M1A0
В	Reject H <sub>0</sub> . There is significant evidence of correlation [no context]	M1A0
C	Sufficient evidence to reject H <sub>0</sub> . There are more computer failures when temperatures are higher	M1A1
	["Evidence" used, albeit in wrong sentence, but BOD]	
D	Wrong but validly obtained TS leading consistently to Do not reject H <sub>0</sub> . There is insufficient evidence that there are	M1A1
	more computer failures when temperatures are higher [standard FT]	
E	Wrong but validly obtained TS leading consistently to Do not reject H <sub>0</sub> . There is evidence that the number of computer	M1A0
	failures is not correlated with temperature. [Non-rejection doesn't give positive evidence that $H_0$ is correct. When $H_0$ is	
	not rejected, candidates should aim for a "double negative"]	
F	(from correct TS and CV) Do not reject H <sub>0</sub> . (+ anything) [inconsistent]	M0A0
G	If $H_0$ , $H_1$ the wrong way round, but calculations right: Reject $H_0$ . (+ anything)	M1A0

# Exemplar responses for Q4(e)

	Response	Mark
A	12 is very high so it does cast doubt [relevant comparison needs to be seen]	B0B1
В	The probability is so low that 12 is worrying so it does cast doubt [unclear comparison]	B0B1
С	0.0653 is not equal to 0.12 so probably not valid [don't allow "not equal"]	B1
D	0.0653 is not close to 0.12	B1
Е	12 is much higher than 6.53 so it is not valid [too definite]	B1B0
F	P(= 12) from $B(100, 0.0653) = 0.0166$ which is very small so it does cast doubt	B0B1
G	P(> 12) from $B(100, 0.0653) = 0.00784$ which is very small so it does cast doubt	B0B1
Н	$P(\ge 12)$ from B(100, 0.0653) = 0.00784 which is very small so it does cast doubt	B0B1
I	$P(\ge 12)$ from B(100, 0.0653) = 0.0299 which is small so it casts doubt [0.035 from N(6.53, 6.1036)]	B1B1
J	Expected number is $100 \times 0.0653 = 6.53$ which is very different from 12 so it does cast doubt	B1B1
K	Wrong p, e.g.: 0.142 not far from 0.12 so it does not cast doubt $(0.142 \text{ from Po}(\geq 6), 0.0267 \text{ from Po}(\geq 7)$	B1B1ft
L	Likewise: Expected number is 14.2 which is not very close to 12 so it does cast doubt	B1B1ft
M	Likewise: $P(\le 12)$ from $B(100, 0.142) = 0.319$ which is not too low so it does not cast doubt	B1B1ft

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