



GCE

Further Mathematics B (MEI)

Y414/01: Numerical Methods

Advanced Subsidiary GCE

Mark Scheme for Autumn 2021

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

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Text Instructions

1. Annotations and abbreviations

Annotation in scoris	Meaning
✓ and ✖	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
E	Explanation mark 1
SC	Special case
^	Omission sign
MR	Misread
BP	Blank page
Highlighting	
Other abbreviations in mark scheme	Meaning
E1	Mark for explaining a result or establishing a given result
dep*	Mark dependent on a previous mark, indicated by *. The * may be omitted if only previous M mark.
cao	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working
AG	Answer given
awrt	Anything which rounds to
BC	By Calculator
DR	This indicates that the instruction In this question you must show detailed reasoning appears in the question.

2. Subject-specific Marking Instructions for AS/A Level Further Mathematics B (MEI)

- a a Annotations must be used during your marking. For a response awarded zero (or full) marks a single appropriate annotation (cross, tick, M0 or ^) is sufficient, but not required.

For responses that are not awarded either 0 or full marks, you must make it clear how you have arrived at the mark you have awarded and all responses must have enough annotation for a reviewer to decide if the mark awarded is correct without having to mark it independently.

It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

Award NR (No Response)

- if there is nothing written at all in the answer space and no attempt elsewhere in the script
- OR if there is a comment which does not in any way relate to the question (e.g. 'can't do', 'don't know')
- OR if there is a mark (e.g. a dash, a question mark, a picture) which isn't an attempt at the question.

Note: Award 0 marks only for an attempt that earns no credit (including copying out the question).

If a candidate uses the answer space for one question to answer another, for example using the space for 8(b) to answer 8(a), then give benefit of doubt unless it is ambiguous for which part it is intended.

- b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not always be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.
If you are in any doubt whatsoever you should contact your Team Leader.

c The following types of marks are available.

- M** A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified. A method mark may usually be implied by a correct answer unless the question includes the DR statement, the command words “Determine” or “Show that”, or some other indication that the method must be given explicitly.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.
- B** Mark for a correct result or statement independent of Method marks.
- E** A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

d When a part of a question has two or more ‘method’ steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation ‘dep*’ is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.

e The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only – differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case, please escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.

Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be ‘follow through’. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

f Unless units are specifically requested, there is no penalty for wrong or missing units as long as the answer is numerically correct and expressed either in SI or in the units of the question. (e.g. lengths will be assumed to be in metres unless in a particular question all the lengths are in km, when this would be assumed to be the unspecified unit.)

We are usually quite flexible about the accuracy to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so.

When a value is **given** in the paper only accept an answer correct to at least as many significant figures as the given value.

When a value is **not given** in the paper accept any answer that agrees with the correct value to **2 s.f.** unless a different level of accuracy has been asked for in the question, or the mark scheme specifies an acceptable range.

NB for Specification A the rubric specifies 3 s.f. as standard, so this statement reads “3 s.f.”

Follow through should be used so that only one mark in any question is lost for each distinct accuracy error.

Candidates using a value of 9.80, 9.81 or 10 for g should usually be penalised for any final accuracy marks which do not agree to the value found with 9.8 which is given in the rubric.

g Rules for replaced work and multiple attempts:

If one attempt is clearly indicated as the one to mark, or only one is left uncrossed out, then mark that attempt and ignore the others.

If more than one attempt is left not crossed out, then mark the last attempt unless it only repeats part of the first attempt or is substantially less complete.

If a candidate crosses out all of their attempts, the assessor should attempt to mark the crossed out answer(s) as above and award marks appropriately.

h For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A or B mark in the question. Marks designated as cao may be awarded as long as there are no other errors. If a candidate corrects the misread in a later part, do not continue to follow through. E marks are lost unless, by chance, the given results are established by equivalent working. Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

i If a calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers provided that there is nothing in the wording of the question specifying that analytical methods are required such as the bold “In this question you must show detailed reasoning”, or the command words “Show” and “Determine. Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.

j If in any case the scheme operates with considerable unfairness consult your Team Leader.

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Mark Scheme

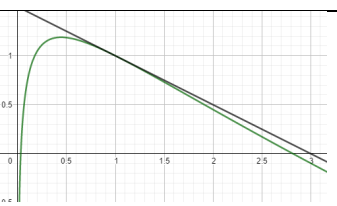
November 2021

Question			Answer	Marks	AOs		Guidance
				[4]			
2	(b)		the calculation involves the subtraction of nearly equal numbers in the denominator oe	B1	2.2a	just subtraction of nearly equal numbers is insufficient	
				[1]			
2	(c)		Amir is wrong because the order of the sequence of operations has been changed oe	B1	2.4	allow eg it's a different calculation	just it's not subtraction of nearly equal numbers is insufficient
				[1]			
3	(a)		$\frac{1.558068-1.386294}{0.1}$ or $\frac{1.471572-1.386294}{0.05}$ soi	M1	1.1		
			1.71774	A1	1.1		
			1.70556	A1	1.1		
				[3]			
	(b)		the data must be (equally spaced) <i>either side</i> of 2 oe	B1	2.4		
				[1]			
	(c)		central difference method is 2 nd order method whereas forward difference is 1 st order method oe	B1	2.4	allow eg central difference method usually more accurate oe	
				[1]			

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Question			Answer	Marks	AOs		Guidance
4	(a)			B1	2.4	tangent from (1,1) cutting the x -axis at (3,0)	allow tangent cutting x -axis between (but not touching) the curve and $x = 3.2$
				[1]			
4	(b)		$f(2.8179205)$ and $f(2.8179215)$ evaluated	M1	1.1	must be fully evaluated, not just substituted	
			0.000 000 34(336) and $-0.000\ 000\ 195(334)$ sign change so correct to 6 dp	A1	2.2a		
				[2]			
4	(c)		the ratios of differences are decreasing (rapidly) so	B1	2.2a		
			the convergence is faster than 1 st order	B1	2.2b		
				[2]			
4	(d)		#NUM! is displayed when the spreadsheet is unable to compute a value oe	B1	1.1		
			in this case it is because it is not possible to find the natural logarithm or square root of a negative number	B1	1.1		
				[2]			

Question			Answer	Marks	AOs	Guidance									
4	(e)		<table><tr><td>N</td><td>O</td><td>P</td><td>Q</td></tr><tr><td>0.01</td><td>− 0.90517</td><td>0.03112</td><td>0.00098</td></tr></table>	N	O	P	Q	0.01	− 0.90517	0.03112	0.00098	B1	1.1		
			N	O	P	Q									
0.01	− 0.90517	0.03112	0.00098												
			$\frac{0.01 \times 0.00098 - -0.90517 \times 0.03112}{0.00098 - -0.90517}$ soi	M1	1.1										
			<table><tr><td>R</td><td>S</td></tr><tr><td>0.03110</td><td>0.00033 − 0.00040</td></tr></table>	R	S	0.03110	0.00033 − 0.00040	A1	1.1						
R	S														
0.03110	0.00033 − 0.00040														
				A1	1.1										
				[4]											
4	(f)		0.0311 since last two estimates agree to this precision	B1	2.2b										
				[1]											
4	(g)		=IF(S8<0,R8,N8) or =IF(S8>0,N8,R8)	B1	1.1	must see =									
				[1]											
5	(a)		$S_{2n} = 2.296296296$	B1	1.1	D2									
			difference = −0.04003(1213)	B1	1.1	E3									
			ratio = 0.1317(47194...)	B1	1.1	awrt 0.1375 NB F4									
			$\frac{2.264070598 + 2M_8}{3} = 2.250517186$	M1	3.1a	or $\frac{2.264070598 + M_8}{2} = 2.253905539$									

Question			Answer	Marks	AOs		Guidance
			$M_8 = 2.24374048$	A1	1.1	C5	
				[5]			
5	(b)		extrapolation with S_{2n} and difference from table	M1	2.1	eg 2.250483378 and -3.38×10^{-5}	M1M1 only available for extrapolation to infinity from T_{32} or M_{32} with $r = 0.25$
			2.250481181 and -2.2×10^{-6} used	A1	3.1a	may be in partial extrapolation eg to S_{128}	
			$2.250481181 - 2.2 \times 10^{-6} \times \frac{1}{1-r}$	A1	1.1	$r = 0.06499 - 0.065$ or $\frac{1}{16}$	NB 2.25048103
			comparison of their answer from extrapolation with S_{64}	M1	1.1	dependent on award of M1	
			2.250481 is certain or 2.2504810 is possible,	A1	2.2b	allow 2.25048103	must follow extrapolation to infinity from S_{64}
				[5]			
6	(a)		$=(D5 - D4)/D4$ or $= D5/D4 - 1$	B1	1.1	must see =	
				[1]			
6	(b)		$y = nx$	B1	3.3		
				[1]			
6	(c)		$\frac{2.718^5 - e^5}{e^5}$ oe	M1	3.4		
			$-0.000518(286998)$	A1	1.1		
			$5 \times (-0.0001037) = -0.0005185$ so model is a good fit for $n = 5$	A1	3.5a		

Question			Answer	Marks	AOs	Guidance
				[3]		
6	(d)		the model becomes less good as the approximation moves further away from e	B1	3.5b	
				[1]		
6	(e)		−0.000 0259 2 or -2.592×10^{-5}	B1	1.1	
				[1]		
6	(f)		so that (the values in cells) F18 and G18 are also multiplied by (the value in cell) D21	B1	2.4	allow “absolute cell reference”
				[1]		
6	(g)		$z = \frac{x}{n}$ oe	B1	3.5c	
				[1]		
7	(a)		$\frac{g(1.875) - g(1.865)}{0.01}$ soi	M1	1.1	NB $\frac{0.010408 - -0.00728}{0.01}$
			awrt 0.424	A1	1.1	0.424(18146683)
				[2]		
7	(b)		this suggests the iteration will converge to the root because $-1 < g'(1.87) < 1$ so she will use the iteration	B1	2.2b	FT their value
				[1]		
7	(c)		P12 = O12 – O11	B1	1.1	if B0B0 allow SC1 for O12 – O11 and P13/P12
			Q13 =P13/P12	B1	1.1	
				[2]		
7	(d)		ratio is tending towards constant (0.424)	B1	1.1	
			which suggests 1 st order convergence	B1	2.2b	
				[2]		

Question			Answer	Marks	AOs		Guidance					
7	(e)		comparison of last two estimates	M1	2.4	if M0 allow SC1 for either 1.869 is certain or 1.8691 is possible with insufficient reasoning						
			1.869 is certain or 1.8691 is possible	A1	2.2b							
				[2]								
7	(f)		<table border="1"><tr><td>2</td></tr><tr><td>1.86893356</td></tr><tr><td>1.86912211</td></tr><tr><td>1.86912218</td></tr><tr><td>1.86912218</td></tr></table>	2	1.86893356	1.86912211	1.86912218	1.86912218	M1	1.1	at least one iterate found using relaxed iteration x_1, x_2 correct to 8 dp	allow justification by calculation of sign change
		2										
		1.86893356										
		1.86912211										
		1.86912218										
		1.86912218										
	A1	1.1										
		1.86912218 [since $x_4 = x_3$] cao	A1	1.1	must see 8 th dp justified by repeat							
				[3]								

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