



Please write clearly in block capitals.

Centre number

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Candidate number

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Surname

Forename(s)

Candidate signature

I declare this is my own work.

AS

FURTHER MATHEMATICS

Paper 2 Discrete

Thursday 14 May 2020

Afternoon

Time allowed: 1 hour 30 minutes

Materials

- You must have the AQA formulae and statistical tables booklet for A-level Mathematics and A-level Further Mathematics.
- You should have a scientific calculator that meets the requirements of the specification. (You may use a graphical calculator.)
- You must ensure you have the other optional Question Paper/Answer Book for which you are entered (**either** Mechanics **or** Statistics). You will have 1 hour 30 minutes to complete **both** papers.

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer each question in the space provided for that question. If you require extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do **not** write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 40.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.

For Examiner's Use	
Question	Mark
1	
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7	
8	
TOTAL	



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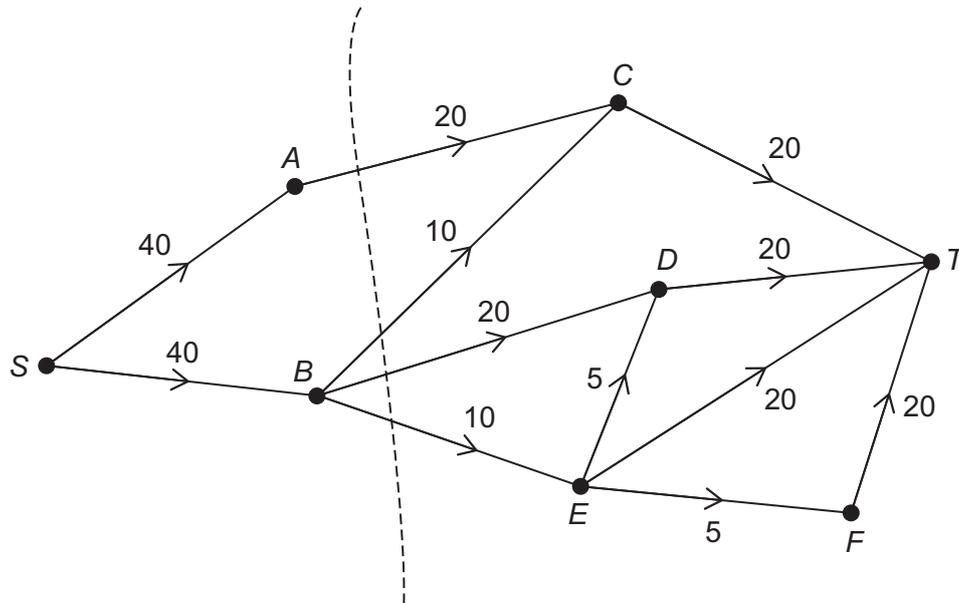
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Answer **all** questions in the spaces provided.

1 The network represents a system of pipes.

The number on each arc represents the upper capacity for each pipe in $\text{cm}^3 \text{s}^{-1}$



The value of the cut $\{S, A, B\} \{C, D, E, F, T\}$ is $60 \text{ cm}^3 \text{ s}^{-1}$

The maximum flow through the system is $M \text{ cm}^3 \text{ s}^{-1}$

What does the value of the cut imply about M ?

Circle your answer.

[1 mark]

$M < 60$

$M \leq 60$

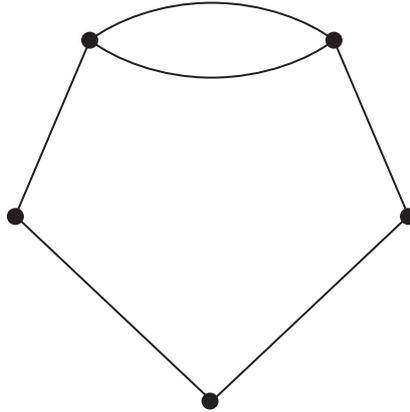
$M \geq 60$

$M > 60$



2

The graph G has 5 vertices and 6 edges, as shown below.



Which of the following statements describes the properties of G ?

Tick (✓) **one** box.

[1 mark]

G is Eulerian and Hamiltonian.

G is Eulerian but not Hamiltonian.

G is semi-Eulerian and Hamiltonian.

G is semi-Eulerian but not Hamiltonian.

Turn over for the next question

Turn over ►



3 (b) (i) State the value of the game for Summer.

[1 mark]

3 (b) (ii) State the play-safe strategy for each player.

[1 mark]

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0 7

5 A restoration project is divided into a number of activities.

The duration and predecessor(s) of each activity are shown in the table below.

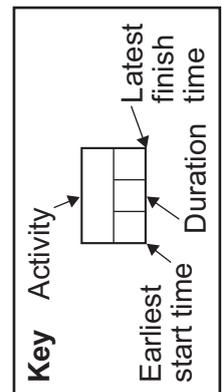
Activity	Immediate predecessor(s)	Duration (weeks)
<i>A</i>	–	10
<i>B</i>	–	5
<i>C</i>	<i>B</i>	12
<i>D</i>	<i>A</i>	8
<i>E</i>	<i>C, D</i>	4
<i>F</i>	<i>C, D</i>	3
<i>G</i>	<i>C, D</i>	7
<i>H</i>	<i>E, F</i>	8
<i>I</i>	<i>G</i>	6
<i>J</i>	<i>G</i>	15
<i>K</i>	<i>H, I</i>	5
<i>L</i>	<i>K</i>	4

5 (a) On the opposite page, construct an activity network for the project and fill in the earliest start time and latest finish time for each activity.

[4 marks]



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1 1

6 A garden has seven statues *A, B, C, D, E, F* and *G*, with paths connecting each pair of statues, either directly or indirectly.

To provide better access to all the statues, some of the paths are being made wider.

6 (a) State why **six** is the minimum number of paths that need to be made wider.

[2 marks]

6 (b) The table below shows the number of trees that need to be removed to make the path between adjacent statues wider.

A dash in the table means that there is no direct path between the two statues.

Statue	<i>A</i>	<i>B</i>	<i>C</i>	<i>D</i>	<i>E</i>	<i>F</i>	<i>G</i>
<i>A</i>	–	4	7	–	–	–	–
<i>B</i>	4	–	6	2	3	–	–
<i>C</i>	7	6	–	–	3	–	4
<i>D</i>	–	2	–	–	4	5	–
<i>E</i>	–	3	3	4	–	3	7
<i>F</i>	–	–	–	5	3	–	6
<i>G</i>	–	–	4	–	7	6	–

Find the minimum number of trees that need to be removed.

Fully justify your answer.

[3 marks]



7 Robyn manages a bakery.

Each day the bakery bakes 900 rolls, 600 teacakes and 450 croissants.

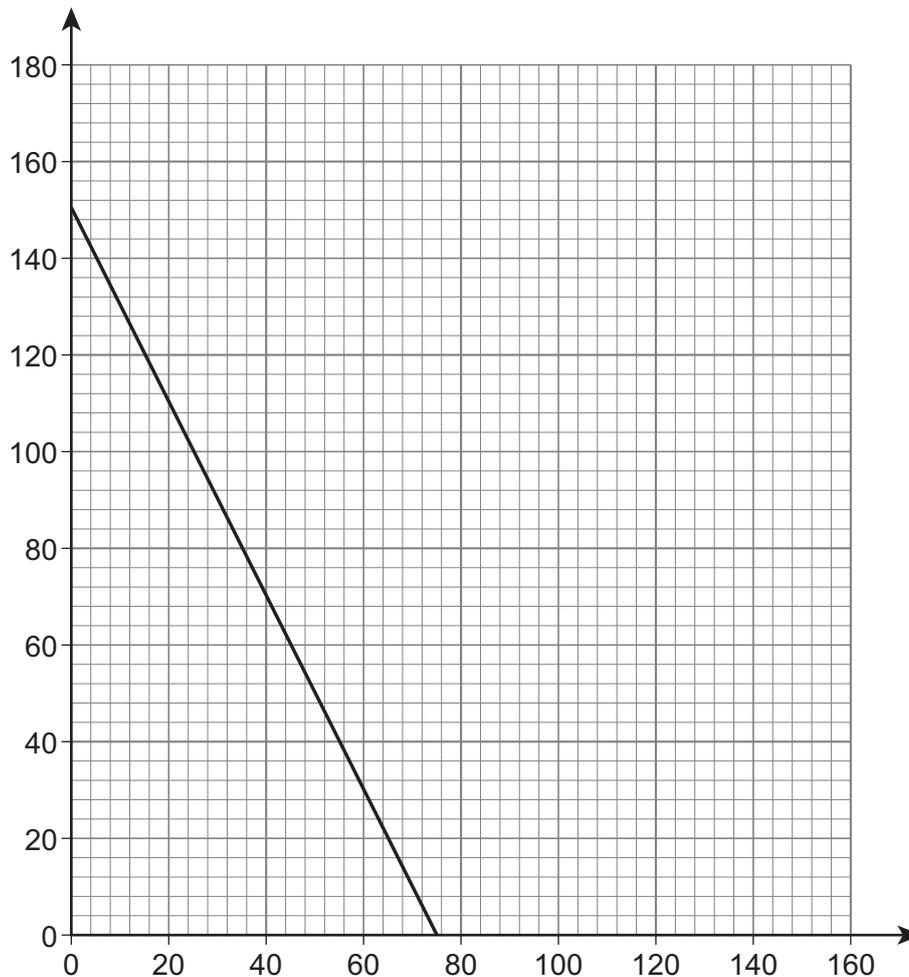
The bakery sells two types of bakery box which contain rolls, teacakes and croissants, as shown in the table below.

Type of bakery box	Number of rolls	Number of teacakes	Number of croissants	Profit per box sold
Standard	12	6	3	£2.50
Luxury	6	6	9	£2.00

Robyn formulates a linear programming problem to find the maximum profit the bakery can make from selling the bakery boxes.

7 (a) Part of a graphical method to solve this linear programming problem is shown on **Figure 1**.

Figure 1



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1 7

8 The set S is defined as

$$S = \{a, b, c, d\}$$

Figure 2 shows a Cayley table for S under the commutative binary operation \odot

Figure 2

\odot	a	b	c	d
a	a	a	a	a
b	a	d	b	c
c	a	b	c	d
d	a	c	d	a

8 (a) (i) Prove that there exists an identity element for S under the binary operation \odot [2 marks]

8 (a) (ii) State the inverse of b under the binary operation \odot [1 mark]



8 (b) Figure 3 shows a Cayley table for multiplication modulo 4

Figure 3

\times_4	0	1	2	3
0	0	0	0	0
1	0	1	2	3
2	0	2	0	2
3	0	3	2	1

Mali says that, by substituting suitable distinct values for a, b, c and d , the Cayley table in **Figure 2** could represent multiplication modulo 4

Use your answers to part (a) to show that Mali's statement is **incorrect**.

[3 marks]

END OF QUESTIONS



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