

Please write clearly in block capitals.	
Centre number	Candidate number
Surname	
Forename(s)	
Candidate signature	

AS **MATHEMATICS**

Paper 2

Wednesday 22 May 2019

Morning

Time allowed: 1 hour 30 minutes

Materials

- You must have the AQA Formulae for A-level Mathematics booklet.
- You should have a graphical or scientific calculator that meets the requirements of the specification.

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer all questions.
- You must answer each question in the space provided for that question.
 If you require extra space, use an AQA supplementary answer book; do not use the space provided for a different question.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.

For Examiner's Use		
Question	Mark	
1		
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13		
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16		
TOTAL		



Section A

Answer all questions in the spaces provided.

Find the gradient of the curve $y = e^{-3x}$ at the point where it crosses the *y*-axis. 1

Circle your answer.

[1 mark]

-3

-1 1

3

Find the centre of the circle $x^2 + y^2 + 4x - 6y = 12$ 2

Tick (✓) one box.

[1 mark]

(-2, -3)



(-2, 3)



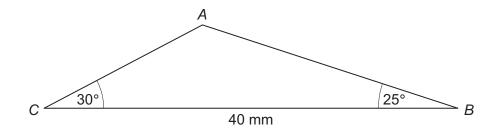
(2, -3)

(2, 3)

lt	is given that $\sin heta = -0.1$ and $180^\circ < heta < 270^\circ$	
Fi	nd the exact value of $\cos \theta$	[2 mark
		-
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Sł	now that, for $x > 0$	
	$\log_{10} \frac{x^4}{100} + \log_{10} 9x - \log_{10} x^3 \equiv 2(-1 + \log_{10} 3x)$	[4 marl
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	Turn over for the next question	



5 A triangular prism has a cross section *ABC* as shown in the diagram below.



Calculate the volume of the prism, giving your answer to three significant figures.

Angle $ABC=25^{\circ}$

Angle $ACB = 30^{\circ}$

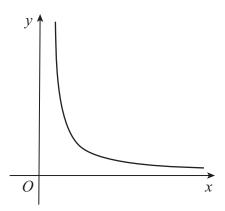
BC = 40 millimetres.

The length of the prism is 300 millimetres.



[4 marks]

6 A curve has equation $y = \frac{2}{x\sqrt{x}}$



The region enclosed between the curve, the x-axis and the lines x=1 and x=a has area 3 units.

Given that a > 1, find the value of a.

Fully justify your answer.	[5 marks]



7	The points $A(a, 3)$ and $B(10, 6)$ lie on a circle.		
	AB is a diameter of the circle and passes through the point (2, 4)		
	The circle has equation		
	$(x-c)^2 + (y-d)^2 = e$		
	where c , d and e are rational numbers.		
	Find the values of a, c, d and e . [6 marks]		
	,		



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Turn over for the next question	
	T



8	A curve has equation	
	$y = x^3 + px^2 + qx - 45$	
	The curve passes through point R (2, 3)	
	The gradient of the curve at R is 8	
8 (a)	Find the value of p and the value of q .	[5 marks]



8 (b)	Calculate the area enclosed between the normal to the curve at R and the convergence	oordinate
	axes.	[5 marks]
		·····
	,	



9	A curve C has equation $y = f(x)$ where
	$f(x) = (x-2)(x-3)^2$
9 (a)	Find the exact coordinates of the turning points of C.
	Determine the nature of each turning point.
	Fully justify your answer.
	[8 marks]



b) State t	ne coordinates of the turning points of the curve	
	y=f(x+1)-4	[2 mark
	Turn over for the next question	
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10	As part of an experiment, Zena puts a bucket of hot water outside on a day when the outside temperature is 0°C.				the
	She measures the temperature of the water at Her results are shown below.	fter 10 m	ninutes ar	nd after 20 minutes.	
	Time (minutes)	10	20		
	Temperature (degrees Celsius)	30	12		
	Zena models the relationship between θ , the the time in minutes, by	emperat	ure of the	e water in $^{\circ}$ C, and t ,	,
	$\theta = A \times 10^{-kt}$				
	where A and k are constants.				
10 (a)	Using $t = 0$, explain how the value of A relate	es to the	experime	ent. [1 m :	ark]
10 (b)	Show that				
	$\log_{10}\theta = \log_{10}A -$	- kt		[1 ma	ark]

10 (c) Using Zena's results, calculate the values of A and k.

[4 marks]

10 (d)	Zena states that the temperature of the water will be less than 1°C after 45 i	minutes.
	Determine whether the model supports this statement.	[3 marks]
10 (e)	Explain why Zena's model is unlikely to accurately give the value of θ after	
	45 minutes.	[1 mark]



		Section B		
	Answer all q	uestions in the spac	es provided.	
11	A survey is undertaken to fine	d out the most popu	lar political party i	n London.
	The first 1100 available peop	le from London are	surveyed.	
	Identify the name of this type	of sampling.		
	Circle your answer.			[1 mark]
	simple random	opportunity	stratified	quota
12	Manny is studying the price a He calculates the value of the price and number of pages in	e product moment c		
	Which of the following best d	escribes the value 1	.05?	
	Tick (✓) one box.			[1 mark]
	definitely correct			
	probably correct			
	probably incorrect			
	definitely incorrect			



Turn over for the next question DO NOT WRITE ON THIS PAGE ANSWER IN THE SPACES PROVIDED

1 5

Turn over ▶

13	Denzel wants to buy a car with a propulsion type other than petrol or diesel.								esel.	
	He takes a sample, from the Large Data Set, of the ${\rm CO_2}$ emissions, in g/km, of cars with one particular propulsion type.									
	The san	nple is a	as follow	/S						
		82	13	96	49	96	92	70	81	
13 (a)	Using you				answer.	a Set, st				e this sample [2 marks]
13 (b)	Calculat	te the m	nean of t	he sam _l	ple.					[1 mark]
13 (c)	Calculat	te the st	tandard	deviatio	n of the	sample.				[1 mark]

13 (d)	Denzel claims that the value 13 is an outlier.				
13 (d) (i)	Any value more than 2 standard deviations from the mean can be regarded as an outlier.				
	Verify that Denzel's claim is correct. [1 mark]				
13 (d) (ii)	State what effect, if any, removing the value 13 from the sample would have on the standard deviation. [1 mark]				
	Turn over for the next question				



14	A probability distribution is given by	
	P(X = x) = c(4 - x), for $x = 0, 1, 2, 3$	
	where c is a constant.	
14 (a)	Show that $c = \frac{1}{10}$	
(-)	10	[2 marks]
14 (b)	Calculate $P(X \ge 1)$	[2 marks]
		[Z marks]



15	Two independent events, A and B , are such that	
	P(A) = 0.2	
	$P(A \cup B) = 0.8$	
15 (a) (i)	Find P(B) [4 mar	·ks]
		_
		_
		_
		_
		_
15 (a) (ii)	Find $P(A \cap B)$ [1 ma	irk]
		_
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15 (b)	State, with a reason, whether or not the events A and B are mutually exclusive. [1 magnetic properties of the events of the events A and B are mutually exclusive.	ark]
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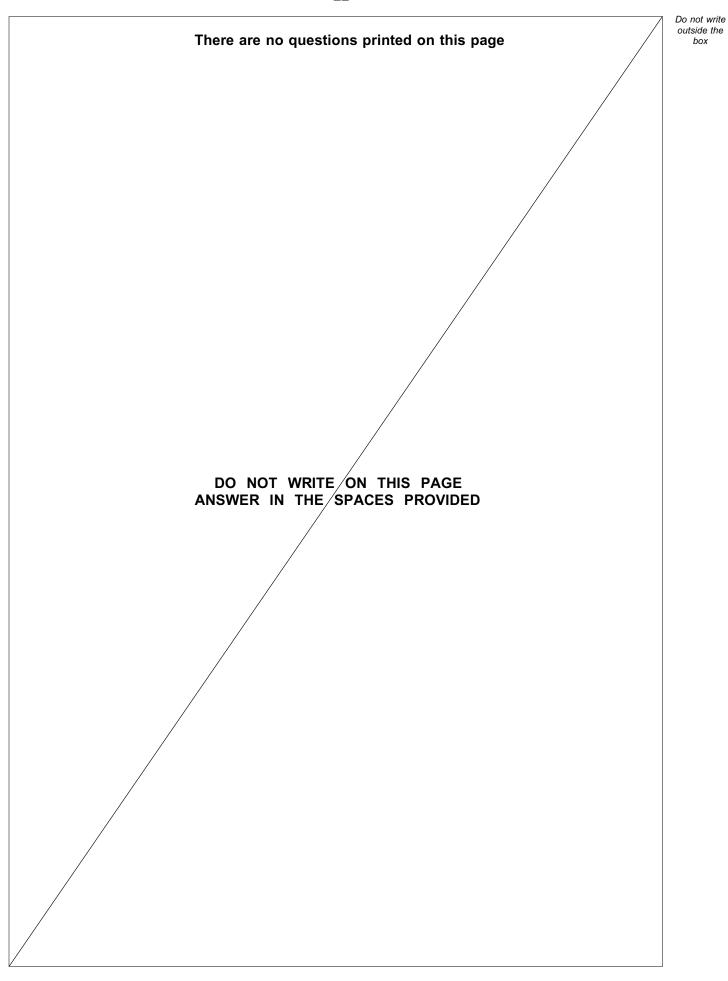


16	Andrea is the manager of a company which makes mobile phone chargers.
	In the past, she had found that 12% of all chargers are faulty.
16 (a)	Andrea decides to move the manufacture of chargers to a different factory.
	Andrea tests 60 of the new chargers and finds that 4 chargers are faulty.
	Investigate, at the 10% level of significance, whether the proportion of faulty chargers has reduced.
	[7 marks]

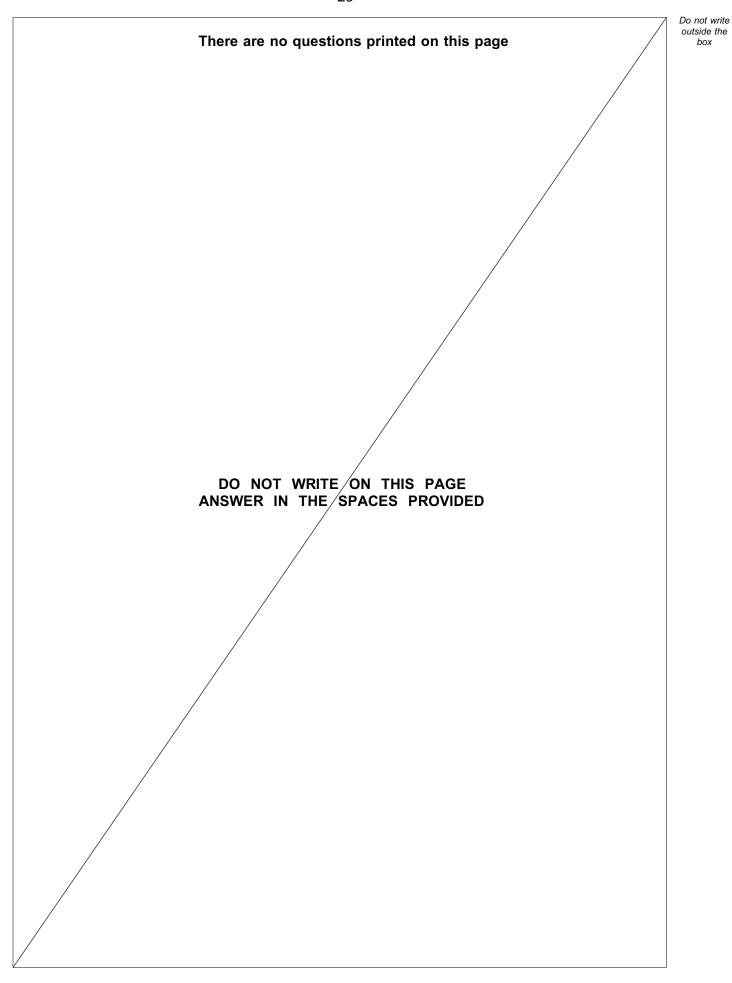


16 (b)	State, in context, two assumptions that are necessary for the distribution that you have used in part (a) to be valid. [2 marks]					
	END OF QUESTIONS					











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