



Please write clearly in block capitals.

Centre number

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Candidate number

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Surname

Forename(s)

Candidate signature

AS FURTHER MATHEMATICS

Paper 2 Discrete

Thursday 16 May 2019

Afternoon

Time allowed: 1 hour 30 minutes

Materials

- You must have the AQA formulae and statistical tables booklet for A-level Mathematics and A-level Further Mathematics.
- You should have a scientific calculator that meets the requirements of the specification. (You may use a graphical calculator.)
- You must ensure you have the other optional Question Paper/Answer Book for which you are entered (**either** Mechanics **or** Statistics). You will have 1 hour 30 minutes to complete **both** papers.

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer each question in the space provided for that question. If you require extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do **not** write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 40.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.

For Examiner's Use	
Question	Mark
1	
2	
3	
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7	
TOTAL	



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PB/Jun19/E2

7366/2D

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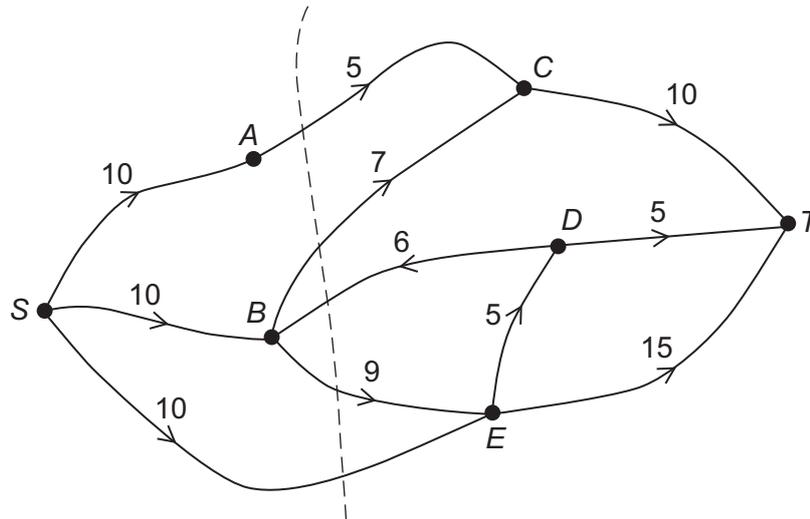


0 2

Answer **all** questions in the spaces provided.

1 The network represents a system of pipes.

The number on each arc represents the upper capacity for each pipe in $\text{cm}^3 \text{s}^{-1}$



The value of the cut $\{S, A, B\} \{C, D, E, T\}$ is $V \text{ cm}^3 \text{ s}^{-1}$

Find V .

Circle your answer.

[1 mark]

25

30

31

37

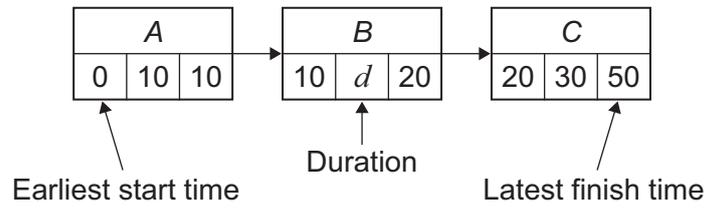
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2 Part of an activity network is shown in the diagram below.

ABC is part of the critical path of the activity network.



The duration of activity B is d .

Which of the following statements about d is correct?

Circle your answer.

[1 mark]

$0 < d < 10$

$d = 10$

$10 < d < 20$

$d = 20$



4 (a) State the definition of a bipartite graph.

[1 mark]

4 (b) A jazz quintet has five musical instruments: bassoon, clarinet, flute, oboe and violin.

Jay, Kay, Lee, Mel and Nish are musicians and each plays a musical instrument in the jazz quintet.

Jay knows how to play the bassoon and the clarinet.

Kay knows how to play the bassoon, the oboe and the violin.

Lee knows how to play the clarinet and the flute.

Mel knows how to play the clarinet, the oboe and the violin.

Nish knows how to play the flute, the oboe and the violin.

4 (b) (i) Draw a graph to show which musicians know how to play which instruments.

[2 marks]



4 (b) (ii) Nish arrives late to a jazz quintet rehearsal.

Each of the other four musicians is already playing an instrument:

- Jay is playing the clarinet
- Kay is playing the oboe
- Lee is playing the flute
- Mel is playing the violin.

Explain how the graph in part **(b)(i)** shows that there is no instrument available that Nish knows how to play.

[1 mark]

4 (b) (iii) When Nish arrives the rehearsal stops. When they restart the rehearsal, Nish is playing the flute.

Draw all possible subgraphs of the graph in part **(b)(i)** that show how Jay, Kay, Lee and Mel can each be assigned a unique musical instrument they know how to play.

[2 marks]

Turn over ►



5 (a) Complete the Cayley table in **Figure 1** for multiplication modulo 4

[2 marks]

Figure 1

\times_4	0	1	2	3
0				
1				
2				
3				

5 (b) The set S is defined as

$$S = \{a, b, c, d\}$$

Figure 2 shows an incomplete Cayley table for S under the commutative binary operation \bullet

Figure 2

\bullet	a	b	c	d
a	b	a	a	c
b		c		c
c		d	d	
d			d	d

5 (b) (i) Complete the Cayley table in **Figure 2**.

[1 mark]



5 (b) (ii) Determine whether the binary operation \bullet is associative when acting on the elements of S .

Fully justify your answer.

[2 marks]

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6 (b) Brook visits every information sign in the nature reserve to update them, **starting and finishing at the entrance**.

For the eight information signs, the minimum connecting distance of the grass paths is 510 metres.

6 (b) (i) Determine a lower bound for the distance Brook walks to visit every information sign.

Fully justify your answer.

[2 marks]

6 (b) (ii) Using the nearest neighbour algorithm **starting from the entrance**, determine an upper bound for the distance Brook walks to visit every information sign.

[2 marks]

Turn over ►



6 (c) Brook takes one minute to update the information at one information sign. Brook walks on the grass paths at an average speed of 5 kilometres per hour. Ashley and Brook start from the entrance at the same time.

6 (c) (i) Use your answers from parts **(a)** and **(b)** to show that Ashley and Brook will return to the entrance at approximately the same time.

Fully justify your answer.

[3 marks]

6 (c) (ii) State an assumption that you have used in part **(c)(i)**.

[1 mark]



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1 3

- 7** Ali and Bex play a zero-sum game.
The game is represented by the following pay-off matrix for Ali.

		Bex		
		Strategy	B₁	B₂
Ali	A₁	2	-1	3
	A₂	-4	-2	2
	A₃	0	1	1
	A₄	-3	2	-2

- 7 (a) (i)** Write down the pay-off matrix for Bex.

[2 marks]

- 7 (a) (ii)** Explain why the pay-off matrix for Bex can be written as

-2	0	3
1	-1	-2

[2 marks]



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