



Please write clearly, in block capitals.

Centre number

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Candidate number

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Surname

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Forename(s)

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Candidate signature

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# A-level FURTHER MATHEMATICS

## Paper 1

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Exam Date

Morning

Time allowed: 2 hours

### Materials

For this paper you must have:

- The AQA booklet of formulae and statistical tables.
- You may use a graphics calculator.

### Instructions

- Use black ink or black ball-point pen. Pencil should be used for drawing.
- Answer **all** questions.
- You must answer each question in the space provided for that question. If you require extra space, use an AQA supplementary answer book; do **not** use the space provided for a different question.
- Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

### Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 100.

### Advice

Unless stated otherwise, you may quote formulae, without proof, from the booklet. You do not necessarily need to use all the space provided.

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Answer **all** questions in the spaces provided.

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1 A vector is given by  $\mathbf{a} = \begin{bmatrix} 2 \\ -1 \\ -3 \end{bmatrix}$

Which vector is **not** perpendicular to  $\mathbf{a}$ ?

Circle your answer.

[1 mark]

$$\begin{bmatrix} 1 \\ -1 \\ 1 \end{bmatrix}$$

$$\begin{bmatrix} 3 \\ 0 \\ 2 \end{bmatrix}$$

$$\begin{bmatrix} 5 \\ -1 \\ 3 \end{bmatrix}$$

$$\begin{bmatrix} 2 \\ 1 \\ 1 \end{bmatrix}$$

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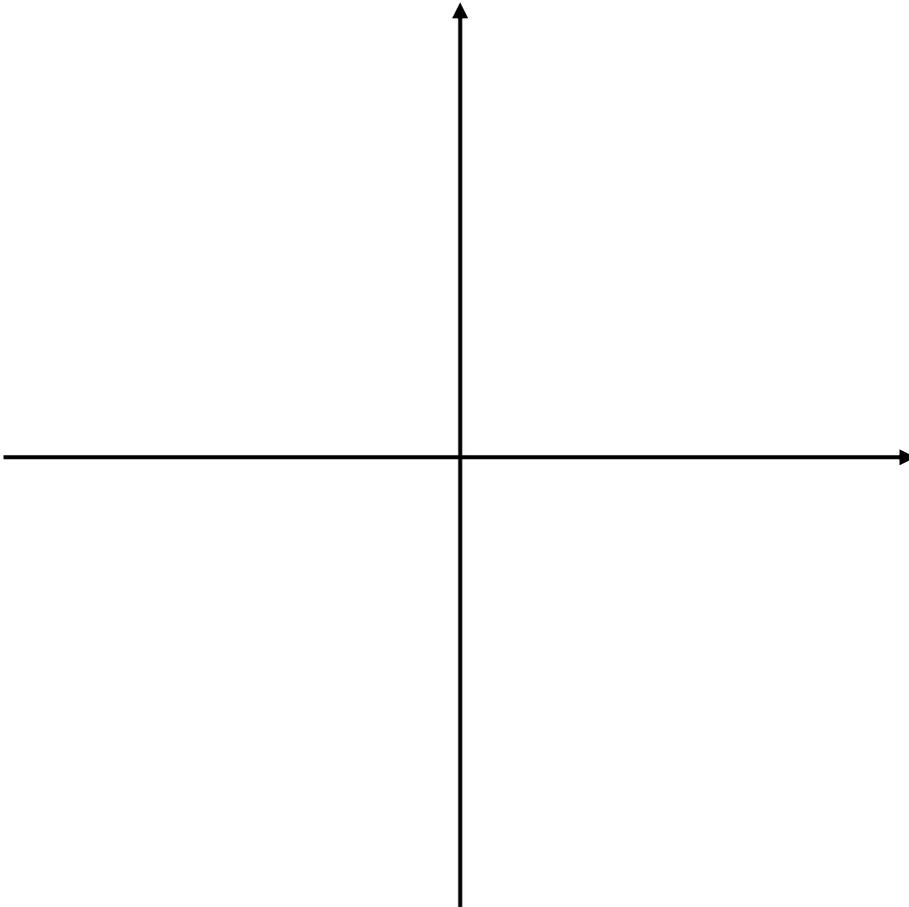


**8** A curve has equation

$$y = \frac{5 - 4x}{1 + x}$$

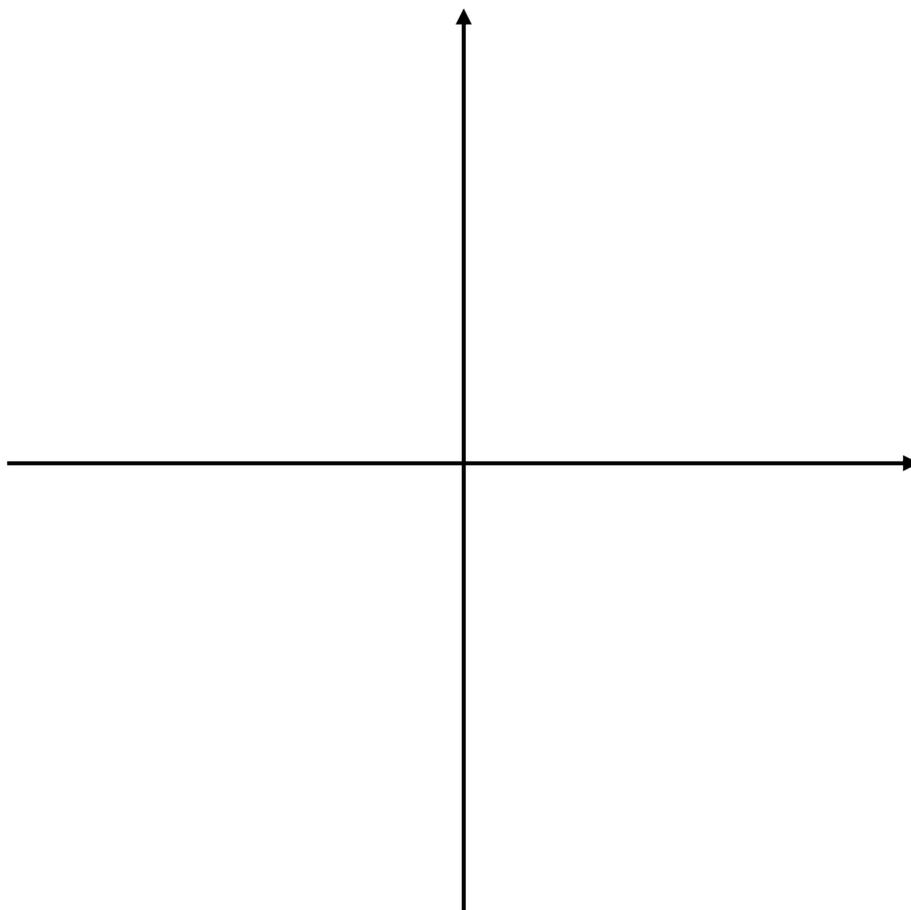
**8 (a)** Sketch the curve.

**[4 marks]**



8 (b) Hence sketch the graph of  $y = \left| \frac{5 - 4x}{1 + x} \right|$ .

[1 mark]



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**9** A line has Cartesian equations  $x - p = \frac{y + 2}{q} = 3 - z$  and a plane has

equation  $\mathbf{r} \cdot \begin{bmatrix} 1 \\ -1 \\ -2 \end{bmatrix} = -3$

**9 (a)** In the case where the plane fully contains the line, find the values of  $p$  and  $q$ .

**[3 marks]**

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**9 (b)** In the case where the line intersects the plane at a single point, find the range of values of  $p$  and  $q$ .

**[3 marks]**

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**9 (c)** In the case where the angle  $\theta$  between the line and the plane satisfies  $\sin\theta = \frac{1}{\sqrt{6}}$  and the line intersects the plane at  $z = 0$

**9 (c) (i)** Find the value of  $q$ .

**[4 marks]**

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**9 (c) (ii)** Find the value of  $p$ .

**[3 marks]**

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**10** The curve,  $C$ , has equation  $y = \frac{x}{\cosh x}$

**10 (a)** Show that the  $x$ -coordinates of any stationary points of  $C$  satisfy the equation  $\tanh x = \frac{1}{x}$   
**[3 marks]**

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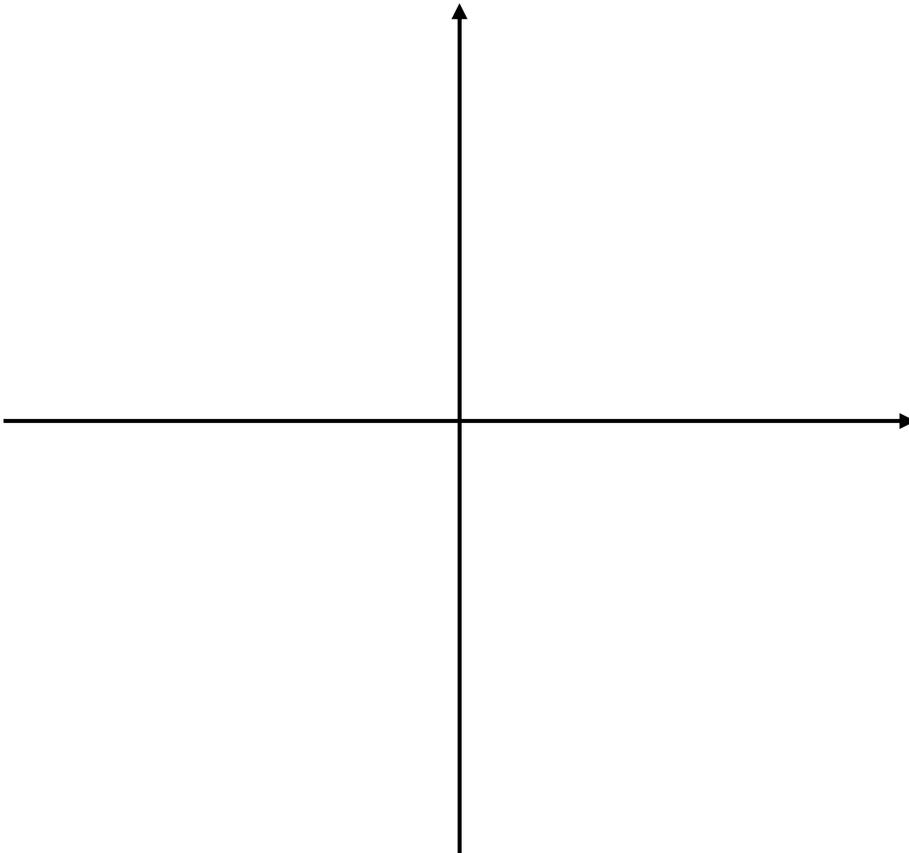
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**10 (b) (i)** Sketch the graphs of  $y = \tanh x$  and  $y = \frac{1}{x}$  on the axes below.

**[2 marks]**



















- 15 (b)** Suggest one way in which the model that you have used for the number of rabbits could be refined.

**[1 mark]**

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**END OF QUESTIONS**